

October 3, 2018

Revised November 16, 2018

Supplemental Information

Generalized-gradient Approximation Exchange Functional with Near-best Semilocal Performance

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In this supplemental material we present:

- a) Detailed analysis of the asymptotic behavior of the NCAP (nearly correct asymptotic potential) exchange potential;
- b) Augmented versions of the tables that appear in the article to report the MD (Mean Deviation) in addition to the MAD (Mean Absolute Deviation);
- c) Plot of satisfaction by NCAP of the global Lieb-Oxford¹ and Perdew *et al.*² bounds;
- d) Comparison of NCAP-shifted HOMO eigenvalue with the system-dependent XC functional of Gledhill and Tozer³ HOMO eigenvalues for small molecules;
- e) Comparison of the NCAP HOMO and LUMO shifted eigenvalues with those from other XC functionals;
- f) Results for the individual molecules of the test sets analyzed

a) Detailed analysis of the asymptotic behavior of the NCAP (nearly correct asymptotic potential) exchange potential

A GGA exchange energy functional usually is expressed in terms of an enhancement factor in the form⁴

$$E_X^{GGA}[n] = \int n(\mathbf{r}) (\varepsilon_X^{LDA}(n(\mathbf{r})) F_X(s)) d\mathbf{r} \quad . \quad (1)$$

Here $\varepsilon_X^{LDA}(n(\mathbf{r})) = A_X (n(\mathbf{r}))^{1/3}$ is the LDA for the exchange energy per particle, $A_X = -3(3\pi^2)^{1/3} / 4\pi$, $n(\mathbf{r})$ is the electron number density, and $s(\mathbf{r}) = |\nabla n(\mathbf{r})| / 2k_F(\mathbf{r})n(\mathbf{r})$, is the exchange reduced density gradient with $k_F = (3\pi^2 n(\mathbf{r}))^{1/3}$.

Since the X potential is given by

$$v_X^{GGA}([n]; \mathbf{r}) = \frac{\delta E_X[n]}{\delta n(\mathbf{r})} \quad , \quad (2)$$

the general expression for the GGA X potential is

$$\begin{aligned} v_X^{GGA}([n]; \mathbf{r}) = & A_X n(\mathbf{r})^{1/3} \left[\frac{4}{3} F_X(s) \right] \\ & + A_X n(\mathbf{r})^{1/3} \left[-\frac{4}{3} s(\mathbf{r}) - \frac{1}{2k_F} \frac{\nabla^2 n(\mathbf{r})}{|\nabla n(\mathbf{r})|} + \frac{1}{2k_F} \frac{\nabla n(\mathbf{r}) \cdot \nabla |\nabla n(\mathbf{r})|}{|\nabla n(\mathbf{r})|^2} \right] \frac{dF_X(s)}{ds} \quad . \quad (3) \\ & + A_X n(\mathbf{r})^{1/3} \left[-\frac{1}{(2k_F)^2} \frac{\nabla n(\mathbf{r}) \cdot \nabla |\nabla n(\mathbf{r})|}{|\nabla n(\mathbf{r})| n(\mathbf{r})} + \frac{4}{3} s(\mathbf{r})^2 \right] \frac{d^2 F_X(s)}{ds^2} \end{aligned}$$

The asymptotic behavior of v_X for a finite system arises only in part from the asymptotic behavior of the density⁵⁻⁷, which very far away from the nucleus is dominated by the exponential decay,

$$n(r) \xrightarrow{r \rightarrow \infty} n_0 e^{-\lambda r} \quad . \quad (4)$$

Using this expression for the density, and the corresponding expressions for the first derivative ($n'(r) \xrightarrow{r \rightarrow \infty} -\lambda n(r)$) and the second derivative ($n''(r) \xrightarrow{r \rightarrow \infty} \lambda^2 n(r)$) of the density with respect to the distance r , Eq. (3) becomes

$$v_X^{GGA}([n]; \mathbf{r}) \xrightarrow{r \rightarrow \infty} A_X n(r)^{1/3} \left[\frac{4}{3} F_X + \left(-\frac{4}{3} s(r) + \frac{1}{k_F r} \right) \frac{dF_X}{ds} + \frac{(s(r))^2}{3} \frac{d^2 F_X}{ds^2} \right] \quad , \quad (5)$$

where $s \xrightarrow{r \rightarrow \infty} \lambda n^{-1/3}(r) / (2(3\pi^2)^{1/3})$. Notice that the $1/k_F r$ coefficient of dF_x / ds in Eq. (5) is structural in the sense that it arises from the Laplacian in spherical polar coordinates in such a fashion that the asymptotic behavior of the density appears only through the coefficient and the spherical symmetry assumed in Eq. (4).

Setting the right-hand side of Eq. (5) equal to $-1/r$ yields a differential equation for the large- r , hence large- s behavior of F_X . Consider what asymptotic potential behavior emerges from the structural contribution of Eq. (5). In conjunction with the simplest possible large- s form of $F_X^{GGA}(s)$, namely $F_X(s) \xrightarrow{s \rightarrow \infty} C_0 s$ with C_0 a constant,⁸ one gets

$$v_X^{GGA}([n]; \mathbf{r}) \xrightarrow{r \rightarrow \infty} -\frac{3 C_0}{4 \pi} \frac{1}{r} \quad (6)$$

or $C_0 = 4\pi/3$ to deliver the desired X potential asymptotic decay. Note that this constant is completely independent of the density details, an explicit indication of the structural nature of this result.

Another possible solution for the asymptotic behavior of the enhancement factor is $F_X(s) \xrightarrow{s \rightarrow \infty} C_1 s \ln s$. Substituting Eq. (4) in the natural logarithm of the reduced density gradient one finds that $\ln s \xrightarrow{r \rightarrow \infty} \lambda r / 3 + \ln(\lambda / (2(3\pi^2 n_0)^{1/3}))$, so that Eq. (5) becomes

$$v_X^{GGA}([n]; \mathbf{r}) \xrightarrow{r \rightarrow \infty} \frac{3 C_1}{4 \pi} \left(\frac{\lambda}{6} - \frac{1 + C_A}{r} \right) \quad , \quad (7)$$

With the choice $C_1 = 4\pi/3$ and the recognition that

$$\lambda = 2\sqrt{-2\varepsilon_H} \quad , \quad (8)$$

where ε_H is the HOMO eigenvalue, the result is

$$v_X^{GGA}([n]; \mathbf{r}) \xrightarrow{r \rightarrow \infty} \left(\frac{\sqrt{-2\varepsilon_H}}{3} - \frac{1 + C_A}{r} \right) \quad , \quad (9)$$

where

$$C_A = \ln \left(\frac{\sqrt{-2\varepsilon_H}}{(3\pi^2 n_0)^{1/3}} \right) \quad . \quad (10)$$

The expression given in Eq. (9) is the same as Eq. (5) of the main paper. Recovery of the asymptotic behavior from an enhancement factor that goes as $s \ln s$ therefore also requires a reference energy shift. This shift has been discussed in a similar context⁹⁻¹³ and is related to the derivative discontinuity of the KS potential.¹⁴⁻¹⁸ We return to it below. Here we point out that the $-1/r$ contribution in Eq. (9) again is a structural contribution, while the contribution $-C_A/r$ comes from the asymptotic behavior of the density.

The required asymptotic form arises from any linear combination of the two asymptotic s dependences just discussed, $F_X(s) \xrightarrow{s \rightarrow \infty} C_0 s$ and $F_X(s) \xrightarrow{s \rightarrow \infty} C_1 s \ln s$ with $C_0 = C_1 = 4\pi/3$. Thus the new functional, denoted NCAP (Nearly Correct Asymptotic Potential) must have

$$F_x^{NCAP}(s) \xrightarrow{s \rightarrow \infty} \frac{4\pi}{3} [(1-\zeta)s \ln s - \zeta s] \quad , \quad (11)$$

that leads to

$$v_X^{GGA}([n]; \mathbf{r}) \xrightarrow{r \rightarrow \infty} v_X^{NCAP}(\epsilon_H, \zeta) - \frac{(1-\zeta)C_A}{r} - \frac{1-\zeta}{r} - \frac{\zeta}{r} \quad , \quad (12)$$

The constant $v_x^{NCAP}(\epsilon_H, \zeta)$ is system-dependent, as denoted by its dependence on the HOMO eigenvalue of the NCAP potential.

On the other hand, the enhancement factor when $s \rightarrow 0$ is¹⁹

$$F_X^{NCAP}(s) \xrightarrow{s \rightarrow 0} 1 + \mu s^2 + \dots \quad , \quad (13)$$

where $\mu = 0.219514973$ corresponds to the PBE value.

Thus, a GGA enhancement factor which achieves these asymptotic properties and has the proper small- s limit, is (Eq. (8) of the article)

$$F_x^{NCAP}(s) = 1 + \mu \tanh(s) \sinh^{-1}(s) \frac{1 + \alpha((1-\zeta)s \ln(1+s) + \zeta s)}{1 + \beta \tanh(s) \sinh^{-1}(s)} \quad , \quad (14)$$

with $\alpha = 4\pi\beta/3\mu$, $\mu = 0.219514973$, $\beta = 0.018085697$, and $\zeta = 0.304121419$, all fixed through constraint satisfaction (see the details in the article).

b) Augmented versions of the tables that appear in the article to report the MD (Mean Deviation) in addition to the MAD (Mean Absolute Deviation)

Table I. MD and MAD for the exchange, correlation and exchange-correlation energies of the noble gas atoms Ne, Ar, Kr, Xe in Hartrees.

	E_x		E_c		E_{xc}	
	MD	MAD	MD	MAD	MD	MAD
LSDA	4.35	4.35	-1.17	1.17	3.18	3.18
PBE	0.41	0.41	0.06	0.06	0.46	0.46
CAP	0.98	0.98	0.06	0.06	1.04	1.04
NCAP	0.20	0.20	-0.13	0.14	0.06	0.07
SCAN	-0.13	0.14	0.07	0.07	-0.07	0.08
B3LYP	0.38	0.38	-0.27	0.27	0.10	0.11
CAM-B3LYP	0.17	0.17	-0.16	0.16	0.02	0.02

Table II. MD and MAD for the heats of formation of the G3 set in kcal/mol (223 molecules), Barrier heights of the BH76 set of reactions in kcal/mol, binding energy of weakly bonded systems of the WB31 set in kcal/mol, bond distances of the T-96R set in Å and dipole moments of the Hait and Head-Gordon set in Debyes (144 molecules)*

	G3		BH		WB		BD		DM	
	MD	MAD	MD	MAD	MD	MAD	MD	MAD	MD	MAD
LSDA	-118.0	118.3	-14.4	15.5	3.5	3.6	-0.066	0.082	-0.051	0.159
PBE	-20.7	21.2	-8.4	9.9	0.80	1.6	0.018	0.018	-0.084	0.153
CAP	-0.4	9.2	-5.9	7.6	-2.3	2.7	0.022	0.022	-0.067	0.141
NCAP	-2.7	6.0	-6.4	8.0	-1.9	2.4	0.025	0.025	-0.076	0.143
SCAN	-3.7	5.1	-6.7	8.6	1.3	1.6	0.003	0.009	-0.020	0.089
B3LYP	4.8	5.7	-3.6	5.9	-0.3	1.2	0.005	0.011	-0.018	0.075
CAM-B3LYP	0.03	3.2	-3.2	3.7	0.1	1.0	0.003	0.014	0.030	0.067

*The original test set of Hait and Head-Gordon has 152 molecules. However in our calculations eight molecules (BH, CH, CH₂NH, CH₂-singlet, HOF, NaLi, O₃, and SiH) were excluded because independently of the XC functional, the calculations did not converge to the ground state.

Table III. Comparison of the HOMO eigenvalue with the experimental ionization potential²⁰⁻²³ in eV for some of the noble gases. The values for NCAP correspond to the shifted exchange potential.

	Ne	Ar	Kr	Xe	MD	MAD
LSDA	13.56	10.40	9.42	8.42	-5.41	5.41
PBE	13.35	10.29	9.28	8.28	-5.57	5.57
CAP	13.11	10.13	9.15	8.17	-5.73	5.73
NCAP	21.19	17.44	16.19	14.92	1.57	1.76
SCAN	14.00	10.73	9.69	8.62	-5.11	5.11
B3LYP	15.65	11.67	10.47	9.28	-4.10	4.10
CAM-B3LYP	17.67	13.48	12.19	10.89	-2.31	2.31
Hartree-Fock	23.14	16.08	14.26	12.44	0.62	0.62
Exp. IP	21.57	15.76	14.00	12.13		

Table IV. MD and MAD for 17 valence and 23 Rydberg excitation energies in eV for a test set with four molecules. The values for NCAP correspond to the unshifted exchange potential.

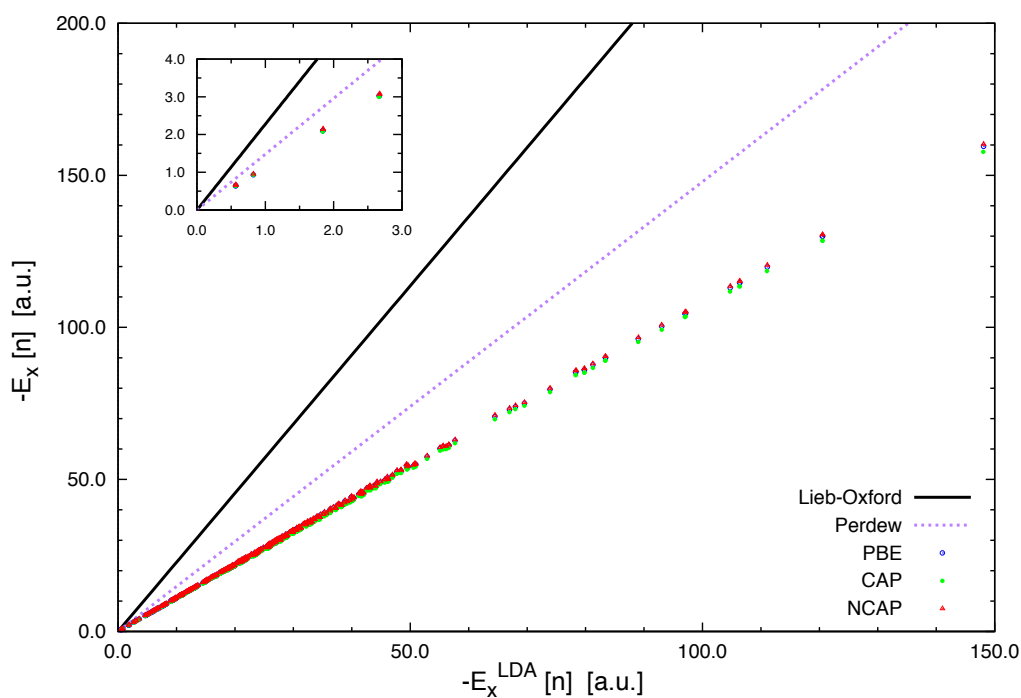
	Valence		Rydberg		Total	
	MD	MAD	MD	MAD	MD	MAD
LSDA	-0.16	0.30	-1.29	1.29	-0.81	0.87
PBE	-0.32	0.35	-1.47	1.47	-0.98	1.00
CAP	-0.28	0.32	-1.25	1.25	-0.84	0.86
NCAP	-0.20	0.26	-0.63	0.64	-0.45	0.48
B3LYP	-0.40	0.40	-0.88	0.88	-0.68	0.68
CAM-B3LYP	-0.41	0.42	-0.46	0.46	-0.44	0.44

c) Plot of satisfaction by NCAP of the global Lieb-Oxford¹ and Perdew *et al.*² bounds

Lieb-Oxford bound¹ $E_X[n_\uparrow, n_\downarrow] \geq -1.679 \int d\mathbf{r} n^{4/3}(\mathbf{r})$

Perdew et al. bound² $E_X[n_\uparrow, n_\downarrow] \geq -1.092 \int d\mathbf{r} n^{4/3}(\mathbf{r})$

The number of cases considered is 492. That total corresponds to the atoms and molecules in the test sets for the heats of formation (G3), barrier heights (BH), weakly bonded systems (WB), bond distances (BD), ionization potentials (IP), electron affinities (EA), proton affinities (PA), and frequencies (F). Specific atoms and molecules are listed in Section h) below.



d) Comparison of NCAP-shifted HOMO eigenvalue with the system-dependent XC functional of Gledhill and Tozer³ HOMO eigenvalues for small molecules

Gledhill and Tozer³ have recently developed an XC functional called ED (for electron deficient) based on density scaling considerations. It contains a Fermi-Amaldi term that leads to an X potential with the correct asymptotic behavior. This functional yields eigenvalues that lie close to the experimental ionization potentials. In the next table we compare the results with the eigenvalues from the shifted NCAP potential and from PBE. One can see that for both functionals, ED and NCAP, the HOMO eigenvalue gets closer to the exact vertical ionization potential.²⁴ Quantities in au.

Molecule	PBE	ED	NCAP	-IP
CH ₄	-0.347	-0.506	-0.604	-0.526
CO	-0.332	-0.515	-0.588	-0.515
Cl ₂	-0.268	-0.414	-0.501	-0.422
F ₂	-0.347	-0.611	-0.579	-0.577
H ₂ O	-0.266	-0.466	-0.499	-0.464
HCl	-0.296	-0.425	-0.528	-0.469
HF	-0.355	-0.593	-0.611	-0.592
N ₂	-0.377	-0.593	-0.634	-0.573
MAD	0.194	0.016	0.051	

e) Comparison of the NCAP HOMO and LUMO shifted eigenvalues with those from other XC functionals

In the following table one can see, for the noble gas atoms, that the NCAP shifted potential leads to LUMO eigenvalues that are negative, whereas in all the other functionals give positive LUMO eigenvalues. HOMO-LUMO eigenvalue differences are similar to those predicted by the other functionals. All quantities are in eV.

Atom		LSDA	PBE	CAP	NCAP	SCAN	B3LYP	CAM-B3LYP	HF
He	H	-15.522	-15.763	-15.528	-24.278	-16.537	-18.004	-19.961	-24.979
	L	1.949	1.786	2.503	-5.353	6.077	1.817	2.443	3.201
Ne	H	-13.552	-13.347	-13.107	-21.19	-13.993	-15.649	-17.671	-23.141
	L	2.887	2.733	3.539	-3.994	3.432	2.807	3.413	4.173
Ar	H	-10.402	-10.285	-10.125	-17.444	-10.732	-11.67	-13.481	-16.082
	L	2.754	2.64	3.553	-3.494	3.642	2.869	3.647	4.708
Kr	H	-9.422	-9.28	-9.147	-16.186	-9.687	-10.473	-12.193	-14.263
	L	0.404	0.405	1.218	-5.822	1.355	0.675	1.544	2.798
Xe	H	-8.423	-8.281	-8.171	-14.922	-8.621	-9.278	-10.887	-12.439
	L	0.277	0.301	1.066	-5.729	1.214	0.566	1.396	2.542
Rn	H	-7.977	-7.83	-7.727	-14.337	-8.139	-8.747	-10.299	-11.646
	L	-0.205	-0.205	0.522	-6.015	0.660	0.008	0.694	1.543

f) Results for the individual molecules of the test sets analyzed

In the following tables we present the individual values for each one of the molecules in the different test sets.

All properties included in the G3/99 test set were calculated at the equilibrium B3LYP/631G(2df,p) structures using B3LYP/6-31G(2df,p) zero-point energies obtained with a frequency scale factor of 0.9854.

The experimental or computational data were taken from Refs. [25-42].

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Table S1: Deviations of the standard enthalpies of formation for the molecules in the G3/99 set obtained with the exchange-correlation functional shown in each column. All quantities are in kcal/mol.

	Molecule	Expt. $\Delta_f H_{298}^o$	Deviation = Theory - Experiment						CAM- B3LYP
			LDA	PBE	CAP	NCAP	SCAN	B3LYP	
1	LiH	33.3	-2.3	5.0	7.8	1.0	3.0	-0.0	-0.6
2	BeH	81.7	-9.3	-4.7	-4.3	-6.8	-9.5	-6.9	-6.9
3	CH	142.5	-8.3	-0.6	1.8	-2.7	2.3	-1.3	-0.5
4	CH ₂ (³ B ₁)	93.7	-22.3	-4.1	-1.8	-5.1	-6.3	-1.8	-2.1
5	CH ₂ (¹ A ₁)	102.8	-17.5	2.2	6.3	-0.8	5.8	0.5	1.2
6	CH ₃	35.0	-31.6	-2.5	2.5	-4.8	-4.7	-2.4	-3.0
7	CH ₄	-17.9	-42.1	0.0	6.4	-2.9	0.7	-0.8	-1.7
8	NH	85.2	-11.3	-4.5	-1.2	-6.7	-0.8	-4.0	-3.1
9	NH ₂	45.1	-25.2	-6.1	-0.4	-9.1	-1.8	-5.4	-4.6
10	NH ₃	-11.0	-38.0	-2.9	4.1	-6.0	4.5	-1.9	-2.0
11	OH	9.4	-16.9	-2.7	-0.4	-3.5	-1.6	-1.1	-1.3
12	H ₂ O	-57.8	-32.4	-0.4	3.1	-1.0	4.6	2.9	1.9
13	FH	-65.1	-20.0	0.1	1.2	0.2	4.8	2.7	1.9
14	SiH ₂ (¹ A ₁)	65.2	-14.6	3.5	5.9	-1.4	2.2	-2.2	-1.9
15	SiH ₂ (³ B ₁)	86.2	-16.4	-1.1	-0.6	-4.6	-7.7	-2.5	-2.8
16	SiH ₃	47.9	-21.4	2.9	5.4	-3.2	-5.0	-3.2	-4.1
17	SiH ₄	8.2	-25.3	8.3	12.5	0.2	-1.3	-1.9	-3.5
18	PH ₂	33.1	-20.7	-1.6	0.9	-6.3	-3.4	-5.6	-5.2
19	PH ₃	1.3	-27.8	2.7	6.1	-3.4	0.7	-2.7	-2.6
20	H ₂ S	-4.9	-23.7	0.5	2.2	-1.8	0.5	0.6	0.7
21	HCl	-22.1	-13.8	0.1	0.6	-0.5	1.5	1.5	1.5
22	Li ₂	51.6	1.0	4.6	9.9	6.7	6.3	3.9	3.7
23	LiF	-80.1	-16.3	0.9	7.7	5.2	5.9	2.8	0.8
24	HCCH	54.2	-53.7	-8.9	1.2	-1.6	4.1	2.6	2.2
25	CH ₂ CH ₂	12.5	-68.7	-8.1	3.9	-3.4	0.9	0.3	-1.0
26	CH ₃ CH ₃	-20.1	-81.7	-4.9	8.8	-2.7	-0.8	0.6	-2.6
27	CN	104.9	-37.5	-15.8	-7.1	-8.7	4.4	2.3	5.6
28	HCN	31.5	-47.4	-13.2	-2.7	-6.8	5.8	-0.2	0.3
29	CO	-26.4	-39.4	-9.6	-3.1	-1.5	5.2	4.1	2.8
30	CHO	10.0	-53.9	-16.4	-8.8	-8.8	-3.1	-1.5	-2.2
31	CH ₂ O	-26.0	-59.7	-12.0	-3.3	-5.8	0.8	0.5	-0.5
32	CH ₃ OH	-48.0	-72.9	-6.9	4.0	-2.8	0.7	1.7	-1.3
33	N ₂	0.0	-38.2	-14.7	-4.2	-9.3	10.0	-0.6	0.3
34	N ₂ H ₄	22.8	-75.6	-13.4	1.4	-11.7	5.4	-4.4	-5.7
35	NO	21.6	-45.7	-19.3	-11.6	-12.6	2.0	-2.2	-2.2
36	O ₂	0.0	-54.6	-23.6	-19.1	-15.3	-7.2	-3.5	-4.1
37	H ₂ O ₂	-32.5	-65.3	-12.7	-4.6	-7.2	2.3	2.4	0.9
38	F ₂	0.0	-39.7	-14.5	-10.8	-8.1	1.1	1.2	1.0
39	CO ₂	-94.1	-83.6	-27.1	-16.6	-10.4	-3.4	1.6	0.3
40	Na ₂	34.0	-3.3	-0.7	7.6	3.8	2.7	0.0	0.8
41	Si ₂	139.9	-16.2	-6.7	-4.3	-3.4	0.1	5.5	11.5
42	P ₂	34.3	-25.8	-4.2	-0.0	-1.9	4.8	1.6	6.4
43	S ₂	30.7	-33.5	-13.7	-11.1	-7.5	-7.8	-1.7	1.4
44	Cl ₂	0.0	-25.0	-7.9	-5.7	-1.9	-0.3	2.3	3.4
45	NaCl	-43.6	-5.4	4.1	7.3	6.9	2.2	5.7	4.5
46	SiO	-24.6	-30.7	-3.2	2.8	2.4	5.9	5.3	4.5
47	CS	66.9	-30.4	-8.3	-3.5	-1.7	4.1	5.1	7.8
48	SO	1.2	-41.6	-15.5	-11.3	-8.3	-5.9	-0.9	-0.5
49	ClO	24.2	-38.8	-16.3	-12.3	-9.6	-4.2	-1.1	0.0
50	ClF	-13.2	-33.2	-10.7	-7.4	-4.3	0.7	1.0	0.6

Table S1 – continued

51	Si ₂ H ₆	19.1	-49.0	10.1	18.7	2.6	-5.9	-0.4	-3.9
52	CH ₃ Cl	-19.6	-52.2	-5.5	2.2	-1.6	-1.3	1.8	0.4
53	CH ₃ SH	-5.5	-62.4	-4.7	4.2	-2.1	-1.2	1.9	0.4
54	HOCl	-17.8	-45.8	-10.6	-5.3	-4.8	0.6	2.0	1.6
55	SO ₂	-71.0	-75.5	-20.6	-11.8	-5.6	-0.1	8.5	7.7
56	BF ₃	-271.4	-77.7	-11.0	3.2	11.1	0.3	6.1	-1.8
57	BCl ₃	-96.3	-59.3	-13.6	-3.8	6.5	-8.7	8.4	5.6
58	AlF ₃	-289.0	-54.7	0.6	14.1	17.7	5.6	11.0	3.0
59	AlCl ₃	-139.7	-37.5	-0.9	7.4	14.6	-6.1	11.3	7.2
60	CF ₄	-223.0	-122.9	-27.9	-11.3	3.0	-4.9	7.4	-3.8
61	CCl ₄	-22.9	-87.8	-21.5	-7.7	6.3	-3.5	15.9	13.0
62	COS	-33.1	-75.3	-26.2	-17.3	-10.9	-7.0	0.3	1.8
63	CS ₂	28.0	-65.8	-23.8	-16.5	-9.9	-8.5	0.9	6.2
64	COF ₂	-149.1	-100.8	-25.3	-11.9	-1.6	-0.9	7.5	1.5
65	SiF ₄	-386.0	-80.9	2.3	19.9	27.2	8.4	17.4	5.4
66	SiCl ₄	-158.4	-59.7	-3.6	7.7	19.8	-6.7	19.1	13.9
67	N ₂ O	19.6	-90.7	-40.2	-26.3	-26.2	-1.2	-5.1	-1.7
68	NOCl	12.4	-74.7	-33.3	-22.6	-21.3	-4.8	-2.0	3.1
69	NF ₃	-31.6	-107.0	-40.3	-26.0	-20.2	-6.2	-2.7	-6.3
70	PF ₃	-229.1	-77.5	-10.3	2.9	8.0	4.1	6.8	-0.8
71	O ₃	34.1	-95.0	-37.8	-28.2	-22.6	-1.1	6.5	9.7
72	F ₂ O	5.9	-78.0	-30.6	-22.1	-17.5	-4.6	-0.6	-1.3
73	ClF ₃	-38.0	-102.2	-39.5	-27.9	-19.4	-11.7	-1.6	-2.3
74	CF ₂ CF ₂	-157.4	-160.9	-47.3	-25.6	-8.8	-12.8	0.4	-9.7
75	CCl ₂ CCl ₂	-3.0	-122.3	-35.0	-16.2	1.5	-10.7	13.7	10.3
76	CF ₃ CN	-118.4	-150.1	-41.9	-16.2	-5.0	-1.7	5.6	-2.9
77	CH ₃ CCH(propyne)	44.2	-96.3	-15.8	1.2	-3.2	0.8	2.5	0.1
78	CH ₂ CCH ₂ (allene)	45.5	-101.4	-20.6	-3.4	-7.8	-3.1	-1.0	-2.3
79	C ₃ H ₄ (cyclopropene)	66.2	-101.4	-18.7	-2.7	-4.4	0.5	4.3	1.1
80	CH ₃ CHCH ₂ (propylene)	4.8	-109.8	-13.3	6.2	-3.0	-1.3	1.9	-1.8
81	C ₃ H ₆ (cyclopropane)	12.7	-115.0	-15.4	2.9	-3.3	-3.0	3.5	-2.0
82	C ₃ H ₈ (propane)	-25.0	-121.4	-9.0	12.6	-1.0	-2.1	3.0	-2.8
83	C ₄ H ₆ (1,3-butadiene)	26.3	-137.8	-22.2	3.2	-3.8	-2.6	2.9	-0.3
84	C ₄ H ₆ (2-butyne)	34.8	-137.7	-21.7	2.3	-3.8	-1.5	3.5	-0.9
85	C ₄ H ₆ (methylene cyclopropane)	47.9	-147.1	-28.0	-4.4	-8.0	-6.9	1.4	-4.0
86	C ₄ H ₆ (bicyclobutane)	51.9	-147.2	-25.0	-2.1	-2.7	-4.0	8.6	1.2
87	C ₄ H ₆ (cyclobutene)	37.4	-142.7	-22.7	0.8	-2.0	-2.4	7.3	1.3
88	C ₄ H ₈ (cyclobutane)	6.8	-154.9	-19.1	6.7	-0.9	-4.4	6.7	-1.6
89	C ₄ H ₈ (isobutene)	-4.0	-150.2	-17.4	10.2	-1.0	-2.8	4.7	-1.6
90	C ₄ H ₁₀ (butane)	-30.0	-160.9	-12.9	16.6	0.8	-3.6	5.5	-2.8
91	C ₄ H ₁₀ (isobutane)	-32.1	-160.8	-11.9	18.2	2.3	-2.8	6.8	-1.8
92	C ₅ H ₈ (spiropentane)	44.3	-189.8	-32.0	-1.7	-4.4	-7.8	7.4	-2.5
93	C ₆ H ₆ (benzene)	19.7	-205.4	-42.2	-6.3	-3.8	-9.7	6.3	-0.5
94	CH ₂ F ₂	-107.7	-80.5	-14.4	-2.9	-1.5	-1.6	2.0	-3.3
95	CHF ₃	-166.6	-101.6	-21.3	-7.0	0.6	-3.1	4.6	-3.5
96	CH ₂ Cl ₂	-22.8	-63.4	-11.0	-1.5	0.5	-1.9	5.7	3.9
97	CHCl ₃	-24.7	-75.3	-16.4	-4.8	3.2	-2.8	10.5	8.2
98	CH ₃ NH ₂ (methylamine)	-5.5	-77.8	-8.1	6.1	-6.2	2.5	-1.3	-3.6
99	CH ₃ CN(acetonitrile)	18.0	-89.6	-19.8	-2.3	-8.2	2.8	-0.2	-1.7
100	CH ₃ NO ₂ (nitromethane)	-17.8	-142.1	-41.0	-19.9	-21.2	-5.6	-1.0	-3.4
101	CH ₃ ONO(methyl nitrite)	-15.9	-137.5	-38.7	-16.9	-19.8	-4.5	-0.2	-2.8
102	CH ₃ SiH ₃ (methyl silane)	-7.0	-63.0	5.2	16.7	2.5	-1.3	1.6	-2.2
103	HCOOH(formic acid)	-90.5	-96.2	-21.3	-7.7	-6.6	-2.2	2.7	-0.9
104	HCOOCH ₃ (methyl formate)	-85.0	-136.6	-26.7	-5.0	-6.9	-6.0	2.7	-3.3
105	CH ₃ CONH ₂ (acetamide)	-57.0	-142.0	-26.9	-2.0	-8.5	-2.9	0.9	-4.6
106	C ₂ H ₄ NH(aziridine)	30.2	-110.7	-19.9	-1.2	-8.5	-0.7	0.9	-3.2

Table S1 – continued

107	C ₂ N ₂ (cyanogen)	73.3	-97.0	-35.8	-14.3	-15.0	6.4	-0.6	2.0
108	(CH ₃) ₂ NH(dimethylamine)	-4.4	-118.6	-13.0	9.3	-5.3	0.4	0.1	-4.7
109	CH ₃ CH ₂ NH ₂ (ethylamine)	-11.3	-118.9	-13.5	8.7	-5.7	-0.1	-0.1	-4.9
110	CH ₂ CO(ketene)	-11.4	-94.7	-25.7	-11.8	-10.8	-5.0	-1.2	-2.4
111	C ₂ H ₄ O(oxirane)	-12.6	-105.7	-19.3	-4.1	-6.1	-3.4	3.3	-1.1
112	CH ₃ CHO(acetaldehyde)	-39.7	-101.4	-17.6	-1.2	-5.6	-1.8	1.7	-1.7
113	HCOCHO(glyoxal)	-50.7	-118.7	-29.7	-10.6	-8.4	-1.8	3.1	-0.3
114	CH ₃ CH ₂ OH(ethanol)	-56.2	-113.0	-11.1	7.7	-1.3	-0.8	3.9	-1.8
115	CH ₃ OCH ₃ (dimethyl ether)	-44.0	-113.7	-12.2	7.0	-2.7	-2.6	2.2	-3.3
116	C ₂ H ₄ S(thiirane)	19.6	-95.5	-16.4	-2.9	-4.2	-4.4	4.1	1.6
117	(CH ₃) ₂ SO(dimethyl sulfoxide)	-36.2	-135.9	-18.7	3.3	-2.4	-4.7	7.7	3.2
118	C ₂ H ₅ SH(ethanethiol)	-11.1	-101.8	-8.5	8.2	-0.2	-1.9	4.6	0.7
119	CH ₃ SCH ₃ (dimethyl sulfide)	-8.9	-101.9	-9.8	6.9	-1.7	-2.9	3.7	0.3
120	CH ₂ CHF(vinyl fluoride)	-33.2	-91.6	-17.9	-3.4	-4.8	-3.0	0.2	-3.3
121	C ₂ H ₅ Cl(ethyl chloride)	-26.8	-92.0	-9.7	5.9	-0.1	-2.4	4.2	0.4
122	CH ₂ CHCl(vinyl chloride)	8.9	-85.2	-18.5	-5.1	-6.3	-5.6	-0.5	-2.3
123	CH ₂ CHCN(acrylonitrile)	43.2	-115.3	-26.9	-3.7	-7.5	3.7	2.5	1.4
124	CH ₃ COCH ₃ (acetone)	-51.9	-141.9	-21.8	2.5	-4.0	-3.6	4.0	-2.1
125	CH ₃ COOH(acetic acid)	-103.4	-136.2	-25.2	-3.9	-4.8	-3.9	5.0	-1.5
126	CH ₃ COF(acetyl fluoride)	-105.7	-123.0	-25.3	-6.4	-4.7	-4.2	3.9	-2.3
127	CH ₃ COCl(acetyl chloride)	-58.0	-115.5	-25.4	-7.3	-5.8	-5.9	4.5	1.3
128	CH ₃ CH ₂ CH ₂ Cl(propyl chloride)	-31.5	-131.8	-13.9	9.5	1.4	-4.1	6.5	0.1
129	(CH ₃) ₂ CHOH(isopropanol)	-65.2	-153.2	-14.8	12.4	1.3	-2.2	6.9	-1.6
130	C ₂ H ₅ OCH ₃ (methyl ethyl ether)	-51.7	-154.1	-16.8	10.2	-1.5	-4.7	4.0	-4.1
131	(CH ₃) ₃ N(trimethylamine)	-5.7	-160.0	-17.5	13.6	-3.4	-1.9	2.3	-5.4
132	C ₄ H ₄ O(furan)	-8.3	-171.0	-37.7	-11.0	-5.7	-8.1	6.2	-0.9
133	C ₄ H ₄ S(thiophene)	27.5	-158.1	-34.1	-9.4	-3.3	-7.6	8.8	4.4
134	C ₄ H ₅ N(pyrrole)	25.9	-177.6	-39.3	-9.2	-8.7	-6.1	2.9	-3.6
135	C ₅ H ₅ N(pyridine)	33.6	-202.2	-47.6	-11.2	-9.8	-8.4	2.6	-3.1
136	H ₂	0.0	-3.5	4.9	4.2	-2.6	2.0	-0.6	0.4
137	SH	34.2	-12.6	-1.0	-0.0	-2.5	-1.6	-1.2	-1.0
138	CCH(² A',C _s)	135.1	-42.9	-11.2	-3.4	-3.1	0.1	3.2	3.7
139	CHCH ₂ (² A',C _s)	71.6	-62.1	-13.1	-2.6	-7.3	-5.7	-2.4	-3.1
140	CH ₃ CO(² A',C _s)	-2.4	-95.2	-22.2	-7.1	-9.2	-5.8	-0.7	-3.5
141	CH ₂ OH(² A,C ₁)	-4.1	-67.2	-11.7	-2.0	-6.3	-4.4	-0.8	-3.5
142	CH ₃ O(² A',C _s)	4.1	-59.8	-12.4	-2.7	-7.9	-6.6	-2.9	-4.7
143	CH ₃ CH ₂ O(² A'',C _s)	-3.7	-100.2	-18.4	-0.8	-8.1	-9.2	-2.1	-6.4
144	CH ₃ S(² A',C _s)	29.8	-53.2	-8.4	-0.3	-4.8	-4.8	-1.3	-2.6
145	CH ₃ CH ₂ (² A',C _s)	28.9	-73.8	-8.8	3.5	-5.7	-6.9	-1.9	-4.5
146	(CH ₃) ₂ CH(² A',C _s)	21.5	-115.6	-14.5	5.5	-5.7	-9.0	-0.7	-5.6
147	(CH ₃) ₃ C(t-butyl radical C _{3v})	12.3	-156.1	-18.5	9.6	-3.5	-9.8	2.4	-5.0
148	NO ₂	7.9	-95.8	-42.5	-30.8	-27.3	-8.1	-5.1	-3.5
149	CH ₂ =C=CHCH ₃ (1,2-butadiene)	38.8	-141.2	-25.1	-0.5	-6.9	-4.1	1.0	-2.4
150	CH ₂ =CH-C(CH ₃)=CH ₂ (isoprene)	18.0	-178.4	-25.8	7.9	-1.0	-3.9	6.3	0.2
151	C ₅ H ₁₀ (cyclopentane)	-18.3	-194.4	-20.9	13.4	3.9	-4.6	11.2	-0.2
152	C ₅ H ₁₂ (n-pentane)	-35.1	-200.3	-16.6	20.7	2.8	-4.6	8.3	-2.6
153	C(CH ₃) ₄ (neopentane)	-40.2	-199.8	-13.6	25.3	7.3	-2.9	12.0	0.2
154	C ₆ H ₈ (1,3-cyclohexadiene)	25.4	-213.3	-34.7	3.5	1.0	-6.1	10.8	1.3
155	C ₆ H ₈ (1,4-cyclohexadiene)	25.0	-212.9	-34.2	3.7	1.4	-5.6	11.0	1.0
156	C ₆ H ₁₂ (cyclohexane)	-29.5	-234.8	-23.6	19.6	7.8	-6.4	14.9	0.3
157	C ₆ H ₁₄ (n-hexane)	-39.9	-240.0	-20.7	24.5	4.5	-4.8	10.7	-2.7
158	C ₆ H ₁₄ (3-methyl pentane)	-41.1	-239.9	-18.8	27.6	7.4	-4.8	13.2	-0.7
159	C ₆ H ₅ CH ₃ (toluene)	12.0	-245.6	-46.3	-2.6	-2.0	-11.3	9.2	-0.1
160	C ₇ H ₁₆ (n-heptane)	-44.9	-279.4	-24.5	28.6	6.4	-7.0	13.4	-2.6
161	C ₈ H ₈ (1,3,5,7-cyclooctatetraene)	70.7	-270.2	-51.8	-1.2	0.5	-6.7	13.8	4.2
162	C ₈ H ₁₈ (n-octane)	-49.9	-318.9	-28.4	32.6	8.3	-9.0	16.0	-2.5

Table S1 – continued

163	C ₁₀ H ₈ (naphthalene)	35.9	-341.6	-75.4	-14.8	-2.9	-19.8	13.9	2.2
164	C ₁₀ H ₈ (azulene)	69.1	-343.1	-78.2	-17.6	-6.1	-19.2	14.1	6.4
165	CH ₃ COOCH ₃ (methyl acetate)	-98.4	-175.7	-29.5	-0.1	-3.9	-6.8	6.1	-2.8
166	(CH ₃) ₃ COH (t-butanol)	-74.7	-192.7	-17.2	18.7	5.4	-3.0	11.3	-0.3
167	C ₆ H ₅ NH ₂ (aniline)	20.8	-246.2	-52.6	-8.3	-8.1	-11.1	5.1	-3.2
168	C ₆ H ₅ OH (phenol)	-23.0	-239.9	-50.2	-9.3	-3.5	-11.6	9.6	0.5
169	CH ₂ =CH-O-CH=CH ₂ (divinyl ether)	-3.3	-173.7	-31.6	-1.3	-5.3	-5.3	3.9	-2.4
170	C ₄ H ₈ O (tetrahydrofuran)	-44.0	-186.8	-24.4	7.2	1.8	-5.5	10.0	-1.2
171	C ₅ H ₈ O (cyclopentanone)	-45.9	-216.5	-35.4	1.3	-0.9	-8.0	10.7	-1.2
172	C ₆ H ₄ O ₂ (1,4-benzoquinone)	-29.4	25.3	-60.9	-17.1	-6.0	-9.9	12.4	4.0
173	C ₄ H ₄ N ₂ (pyrimidine)	46.8	-200.0	-54.1	-17.4	-17.0	-8.4	-2.4	-7.4
174	(CH ₃) ₂ SO ₂ (dimethyl sulfone)	-89.2	-168.3	-23.7	2.7	1.4	-7.3	14.2	6.0
175	C ₆ H ₅ Cl (chlorobenzene)	12.4	-217.8	-48.2	-10.6	-2.0	-11.9	10.0	2.7
176	NC-CH ₂ CH ₂ -CN (succinonitrile)	50.1	-174.6	-42.1	-5.6	-10.2	5.3	4.2	-0.1
177	C ₄ H ₄ N ₂ (pyrazine)	46.9	-196.4	-50.5	-13.7	-13.5	-4.2	1.5	-3.1
178	CH ₃ COCCH ₃ (acetyl acetylene)	15.6	-153.3	-31.0	-3.5	-3.1	-0.2	8.3	3.9
179	CH ₃ -CH=CH-CHO (crotonaldehyde)	-24.0	-171.6	-32.8	-3.0	-7.2	-6.5	3.2	-2.3
180	(CH ₃ CO) ₂ O (acetic anhydride)	-136.8	-237.9	-48.5	-9.0	-7.3	-10.7	8.3	-3.4
181	C ₄ H ₆ S (2,5-dihydrothiophene)	20.8	-165.1	-27.5	-0.5	-0.2	-5.8	9.6	2.8
182	CH ₃ CH(CH ₃)CN (2-methyl propanenitrile)	5.6	-165.9	-25.3	8.0	-2.2	2.4	7.1	0.5
183	CH ₃ -CO-CH ₂ CH ₃ (methyl ethyl ketone)	-57.1	-181.8	-25.7	6.5	-2.0	-5.4	6.7	-2.2
184	(CH ₃) ₂ CH-CHO (isobutyraldehyde)	-51.6	-178.9	-23.7	8.8	-0.0	-2.7	8.7	0.1
185	C ₄ H ₈ O ₂ (1,4-dioxane)	-75.5	-220.9	-31.8	6.2	2.6	-8.7	11.6	-2.4
186	C ₄ H ₈ S (tetrahydrothiophene)	-8.2	-174.9	-21.0	8.5	4.1	-5.0	12.7	3.7
187	(CH ₃) ₃ C-Cl (t-butyl chloride)	-43.5	-171.6	-15.7	17.0	6.6	-4.6	11.8	2.3
188	CH ₃ CH ₂ CH ₂ CH ₂ Cl (n-butyl chloride)	-37.0	-170.6	-17.2	14.1	3.9	-3.8	9.7	0.8
189	C ₄ H ₈ NH (pyrrolidine)	-0.8	-192.4	-25.8	9.2	-1.3	-3.2	7.4	-3.1
190	CH ₃ CH ₂ CH(NO ₂)CH ₃ (2-nitrobutane)	-39.1	-260.9	-51.4	-5.7	-13.5	-9.3	8.2	-2.3
191	CH ₃ CH ₂ OCH ₂ CH ₃ (diethyl ether)	-60.3	-193.4	-20.4	14.5	0.7	-5.1	6.8	-3.9
192	CH ₃ -CH(OCH ₃) ₂ (1,1-dimethoxy ethane)	-93.1	-221.1	-21.8	19.2	7.4	-1.7	14.9	1.5
193	(CH ₃) ₃ C-SH (t-butanethiol)	-26.2	-181.5	-14.4	19.6	6.8	-3.8	12.7	3.0
194	(CH ₃ CH ₂ S) ₂ (diethyl disulfide)	-17.9	-201.3	-22.5	12.9	3.0	-7.6	12.9	5.3
195	(CH ₃) ₃ C-NH ₂ (t-butylamine)	-28.9	-197.4	-18.2	21.2	2.4	-1.0	8.7	-2.2
196	Si(CH ₃) ₄ (tetramethyl silane)	-55.7	-175.6	-1.9	32.7	12.6	-0.4	14.7	3.8
197	C ₅ H ₆ S (2-methyl thiophene)	20.0	-198.1	-38.4	-6.0	-1.9	-8.8	11.2	4.5
198	C ₅ H ₇ N (N-methyl pyrrole)	24.6	-217.2	-43.2	-5.2	-7.1	-7.9	5.2	-3.8
199	C ₅ H ₁₀ O (tetrahydropyran)	-53.4	-227.8	-27.5	13.1	5.4	-7.4	13.4	-0.9
200	C ₂ H ₅ COC ₂ H ₅ (diethyl ketone)	-61.6	-222.2	-30.3	9.9	-0.7	-7.4	8.7	-2.8
201	CH ₃ COOCH(CH ₃) ₂ (isopropyl acetate)	-115.1	-255.3	-36.7	9.1	0.9	-8.4	11.9	-2.4
202	C ₅ H ₁₀ S (tetrahydrothiopyran)	-15.2	-215.6	-24.5	13.9	7.2	-6.6	15.8	3.7
203	C ₅ H ₁₀ NH (piperidine)	-11.3	-233.3	-28.8	15.1	2.3	-5.1	10.8	-2.9
204	(CH ₃) ₃ COCH ₃ (t-butyl methyl ether)	-67.8	-233.0	-21.4	23.2	7.0	-5.8	13.1	-1.2
205	C ₆ H ₄ F ₂ (1,3-difluorobenzene)	-73.9	-249.4	-59.6	-18.3	-4.1	-15.8	8.2	-3.1
206	C ₆ H ₄ F ₂ (1,4-difluorobenzene)	-73.3	-249.2	-59.5	-18.3	-4.0	-15.6	8.3	-3.0
207	C ₆ H ₅ F (fluorobenzene)	-27.7	-227.1	-50.6	-12.0	-3.7	-12.4	7.5	-1.5
208	(CH ₃) ₂ CHOCH(CH ₃) ₂ (diisopropyl ether)	-76.3	-272.6	-26.2	25.9	7.5	-6.5	14.4	-2.2
209	PF ₅	-381.1	-123.4	-10.6	10.8	23.4	4.2	18.2	2.5
210	SF ₆	-291.7	-171.6	-32.4	-8.1	13.6	-9.8	20.3	2.2
211	P ₄	14.1	-75.3	-19.5	-11.3	-3.9	-2.6	10.3	16.5
212	SO ₃	-94.6	-110.4	-30.6	-18.2	-7.3	-5.0	11.9	9.5
213	SCl ₂	-4.2	-47.4	-14.8	-9.6	-3.0	-4.6	4.1	6.2
214	POCl ₃	-133.8	-88.5	-17.5	-3.9	7.4	-7.3	14.8	11.6
215	PCl ₅	-86.1	-97.9	-21.9	-6.0	9.3	-14.2	17.7	15.6
216	SO ₂ Cl ₂	-84.8	-115.6	-31.5	-17.2	-2.7	-10.8	15.2	13.8
217	PCl ₃	-69.0	-59.9	-14.7	-5.5	1.7	-6.3	7.2	8.3
218	S ₂ Cl ₂	-4.0	-75.8	-27.5	-19.3	-9.7	-12.7	2.4	7.3

Table S1 – continued

219	SiCl ₂ (¹ A ₁)	-40.3	-35.0	-5.9	0.1	4.4	-2.6	5.7	5.8
220	CF ₃ Cl	-169.5	-115.8	-28.4	-12.3	1.7	-6.7	7.8	-1.3
221	C ₂ F ₆	-321.3	-203.3	-46.6	-15.6	7.3	-10.6	13.2	-5.6
222	CF ₃	-111.3	-97.4	-28.6	-16.1	-5.6	-9.7	0.5	-6.8
223	C ₆ H ₅ (phenyl radical)	81.2	-199.1	-47.8	-13.6	-8.5	-16.4	3.5	-2.3

Table S2: Deviations of the ionization potential for the test set IP13/3 for the exchange-correlation functional shown in each column. All quantities are in kcal/mol.

		Expt.	Deviation = Theory - Experiment						
Molecule			LDA	PBE	CAP	NCAP	SCAN	B3LYP	CAM-B3LYP
1	C	259.7	9.3	6.3	2.9	5.6	9.7	6.2	6.7
2	S	238.9	3.6	0.4	-3.2	3.1	-0.4	3.4	3.1
3	SH	238.9	4.0	-0.4	-4.0	1.1	-0.1	1.8	1.7
4	Cl	299.1	5.2	0.2	-3.5	1.3	1.4	2.3	2.4
5	Cl ₂	265.3	-1.6	-4.2	-7.5	-3.0	1.2	1.3	3.6
6	OH	299.1	9.0	4.2	-1.7	5.1	2.2	6.0	5.8
7	O	313.9	9.1	10.2	2.3	12.4	3.4	12.5	11.5
8	O ₂	278.9	10.1	7.0	3.2	7.8	14.0	14.6	15.1
9	P	241.9	2.2	0.4	-1.6	-0.0	3.7	-2.0	-1.9
10	PH	234.1	3.5	2.5	0.2	2.4	6.5	0.9	1.0
11	PH ₂	226.3	4.1	3.8	1.0	4.0	8.5	2.9	3.1
12	S ₂	216.0	5.1	4.2	1.3	4.8	9.2	7.4	9.0
13	Si	187.9	2.0	1.3	-0.7	1.5	4.1	-0.6	-0.7

Table S3: Deviations of the electron affinities for the test set EA13/3 for the exchange-correlation functional shown in each column. All quantities are in kcal/mol.

		Expt.	Deviation = Theory - Experiment						
Molecule			LDA	PBE	CAP	NCAP	SCAN	B3LYP	CAM-B3LYP
1	C	29.1	12.0	7.0	3.8	6.7	4.6	2.3	1.4
2	S	47.9	6.9	1.8	-2.4	3.4	1.2	2.7	1.7
3	SH	53.3	6.0	0.4	-3.7	1.2	-1.4	0.6	-0.4
4	Cl	83.4	7.8	1.7	-2.3	2.4	1.2	2.2	1.6
5	Cl ₂	55.6	9.7	12.2	7.2	14.5	14.3	16.3	14.5
6	OH	42.1	9.7	0.5	-4.5	1.1	-6.8	-1.5	-1.9
7	O	33.7	11.7	5.1	-1.2	6.2	0.0	3.7	3.3
8	O ₂	10.8	1.5	-0.3	-6.3	1.4	-3.5	3.0	2.3
9	P	17.2	5.4	1.7	-2.3	4.9	-0.3	3.7	2.0
10	PH	23.2	4.9	0.2	-4.1	1.9	-1.7	1.3	-0.2
11	PH ₂	29.4	3.8	-1.4	-5.5	-0.5	-4.0	-1.2	-2.4
12	S ₂	38.5	2.1	-0.1	-4.1	1.4	-0.4	2.6	2.9
13	Si	31.9	4.3	2.0	0.1	2.5	3.2	-1.2	-2.5

Table S4: Deviations of the proton affinities for the test set PA8 for the exchange-correlation functional shown in each column. All quantities are in kcal/mol.

		Expt.	Deviation = Theory - Experiment						
Molecule			LDA	PBE	CAP	NCAP	SCAN	B3LYP	CAM-B3LYP
1	NH ₃	211.9	-4.8	-1.3	1.3	0.5	0.0	-1.0	-2.1
2	H ₂ O	171.8	-4.5	-2.0	0.7	-0.3	-0.7	-2.1	-3.1
3	HCCH	156.6	-2.4	2.6	5.0	4.6	4.0	2.3	1.2
4	SiH ₄	156.5	-8.6	-0.9	0.4	1.8	-2.4	-0.2	-2.9
5	PH ₃	193.1	-9.0	-2.6	-0.7	-0.2	-0.4	-0.3	-1.1
6	H ₂ S	173.7	-5.9	-0.2	1.7	1.8	-0.0	-0.1	-1.8
7	HCl	137.1	-5.6	-0.7	1.4	1.1	-1.4	-1.8	-3.6
8	H ₂	105.9	-4.3	-0.9	1.1	0.3	-1.4	-2.6	-4.0

Table S5: Deviations of the binding energies for the 31 weakly interacting systems for the exchange-correlation functional shown in each column. All quantities are in kcal/mol.

		Expt.	Deviation = Theory - Experiment						
Molecule			LDA	PBE	CAP	NCAP	SCAN	B3LYP	CAM-B3LYP
1	(NH ₃) ₂	3.15	3.32	1.08	-1.68	-1.27	1.21	0.39	0.90
2	(HF) ₂	4.57	3.13	0.73	-2.17	-1.76	1.25	0.43	1.06
3	(H ₂ O) ₂	4.97	4.46	1.56	-1.42	-1.07	1.86	1.03	1.75
4	NH ₃ -H ₂ O	6.41	5.62	2.23	-0.82	-0.51	2.11	1.35	2.03
5	(HCONH ₂) ₂	14.94	6.74	-0.20	-5.29	-4.77	1.18	-1.38	0.13
6	(HCOOH) ₂	16.15	9.34	0.62	-4.32	-4.27	2.05	-0.54	1.36
7	C ₂ H ₄ -F ₂	1.06	3.93	2.30	-0.75	-0.22	1.98	0.55	0.23
8	NH ₃ -F ₂	1.81	6.99	4.66	1.39	1.89	3.65	1.98	1.46
9	C ₂ H ₂ -ClF	3.81	6.33	2.31	-1.47	-0.79	3.36	0.01	-0.26
10	HCN-ClF	4.86	4.97	1.09	-2.56	-1.93	0.72	-0.25	0.16
11	NH ₃ -Cl ₂	4.88	9.02	4.89	1.42	1.85	4.10	2.21	1.70
12	H ₂ O-ClF	5.36	7.10	2.98	-0.77	-0.21	3.41	1.26	1.62
13	NH ₃ -ClF	10.62	14.81	8.09	4.17	4.10	7.99	3.82	2.97
14	(H ₂ S) ₂	1.66	2.29	0.53	-1.76	-1.47	-1.40	-0.40	-0.12
15	(HCl) ₂	2.01	2.18	0.25	-2.23	-1.84	0.75	-0.54	-0.21
16	HCl-H ₂ S	3.35	3.94	1.29	-1.33	-1.05	0.53	0.00	0.23
17	CH ₃ Cl-HCl	3.55	3.13	0.02	-3.46	-2.87	1.85	-1.13	-0.61
18	HCN-CH ₃ SH	3.59	2.49	0.12	-2.96	-2.50	0.90	-0.81	-0.33
19	CH ₃ SH-HCl	4.16	5.83	2.00	-1.44	-1.13	2.33	0.18	0.54
20	HeNe	0.04	0.32	0.28	-0.41	-0.48	0.18	0.13	0.20
21	HeAr	0.06	0.48	0.40	-0.44	-0.49	0.67	0.18	0.29
22	Ne ₂	0.08	0.18	0.15	-0.82	-0.86	0.19	-0.03	0.06
23	NeAr	0.13	0.20	0.06	-1.09	-1.08	0.14	-0.16	-0.04
24	CH ₄ -Ne	0.22	0.22	0.08	-1.25	-1.22	0.34	-0.20	-0.05
25	C ₆ H ₆ -Ne	0.47	0.52	-0.08	-2.69	-2.49	0.22	-0.58	-0.22
26	(CH ₄) ₂	0.51	0.47	-0.50	-2.96	-2.56	0.09	-1.03	-0.62

Table S5 – continued

27	(C ₂ H ₂) ₂	1.34	0.84	-0.24	-2.61	-2.21	-0.55	-0.81	-0.47
28	(C ₂ H ₄) ₂	1.42	1.20	-0.91	-4.71	-3.94	-0.85	-1.74	-1.04
29	Sandwich C ₆ H ₆	1.81	-1.10	-3.80	-8.66	-7.90	-0.97	-4.49	-3.30
30	T-Shaped C ₆ H ₆	2.74	0.13	-2.97	-7.06	-6.64	0.59	-3.35	-2.13
31	Parallel C ₆ H ₆	2.78	-0.69	-4.30	-9.67	-8.85	-1.03	-5.18	-3.71

Table S6: Deviations of the FORWARD barrier heights of hydrogen transfer reactions for the HTBH38/04 test set for the exchange-correlation functional shown in each column. All quantities are in kcal/mol.

		Expt.	Deviation = Theory - Experiment						
Molecule			LDA	PBE	CAP	NCAP	SCAN	B3LYP	CAM-B3LYP
1	$\text{H} + \text{HCl} \rightarrow \text{H}_2 + \text{Cl}$	5.7	-8.9	-5.2	-3.7	-7.7	-7.5	-6.5	-4.7
2	$\text{OH} + \text{H}_2 \rightarrow \text{H} + \text{H}_2\text{O}$	5.7	-23.4	-11.5	-8.3	-6.8	-7.5	-4.8	-4.5
3	$\text{CH}_3 + \text{H}_2 \rightarrow \text{H} + \text{CH}_4$	12.1	-17.4	-8.2	-5.4	-3.8	-4.9	-3.3	-3.2
4	$\text{OH} + \text{CH}_4 \rightarrow \text{CH}_3 + \text{H}_2\text{O}$	6.7	-23.3	-11.8	-8.4	-7.4	-8.0	-4.3	-3.3
5	$\text{H} + \text{H}_2 \rightarrow \text{H}_2 + \text{H}$	9.6	-12.4	-5.9	-5.3	-7.0	-7.2	-5.3	-4.7
6	$\text{OH} + \text{NH}_3 \rightarrow \text{H}_2\text{O} + \text{NH}_2$	3.2	-27.2	-15.3	-11.6	-10.7	-10.6	-5.9	-3.6
7	$\text{HCl} + \text{CH}_3 \rightarrow \text{Cl} + \text{CH}_4$	1.7	-15.1	-7.5	-4.2	-3.7	-4.7	-3.1	-2.1
8	$\text{OH} + \text{C}_2\text{H}_6 \rightarrow \text{H}_2\text{O} + \text{C}_2\text{H}_5$	3.4	-23.7	-11.9	-8.3	-7.3	-8.0	-4.0	-2.8
9	$\text{F} + \text{H}_2 \rightarrow \text{HF} + \text{H}$	1.8	-24.7	-13.7	-10.0	-9.6	-8.9	-7.0	-6.3
10	$\text{O} + \text{CH}_4 \rightarrow \text{OH} + \text{CH}_3$	13.7	-23.2	-13.5	-9.6	-9.6	-11.2	-5.9	-4.7
11	$\text{H} + \text{PH}_3 \rightarrow \text{PH}_2 + \text{H}_2$	3.1	-10.5	-4.8	-3.9	-6.0	-6.1	-4.1	-3.0
12	$\text{H} + \text{HO} \rightarrow \text{H}_2 + \text{O}$	10.7	-12.8	-7.3	-6.7	-9.2	-7.6	-6.9	-5.2
13	$\text{H} + \text{H}_2\text{S} \rightarrow \text{H}_2 + \text{HS}$	3.5	-10.3	-4.7	-3.6	-5.8	-6.3	-4.0	-2.8
14	$\text{O} + \text{HCl} \rightarrow \text{OH} + \text{Cl}$	9.8	-32.6	-20.2	-15.7	-15.6	-14.0	-8.7	-5.5
15	$\text{NH}_2 + \text{CH}_3 \rightarrow \text{CH}_4 + \text{NH}$	8.0	-16.7	-7.6	-4.9	-3.6	-3.6	-2.1	-1.0
16	$\text{NH}_2 + \text{C}_2\text{H}_5 \rightarrow \text{C}_2\text{H}_6 + \text{NH}$	7.5	-13.6	-4.9	-2.0	-0.7	-1.6	0.5	1.4
17	$\text{C}_2\text{H}_6 + \text{NH}_2 \rightarrow \text{NH}_3 + \text{C}_2\text{H}_5$	10.4	-20.0	-8.9	-5.4	-4.1	-5.7	-1.6	-0.6
18	$\text{NH}_2 + \text{CH}_4 \rightarrow \text{CH}_3 + \text{NH}_3$	14.5	-20.6	-10.1	-6.9	-5.6	-6.8	-3.2	-2.2
19	$\text{C}_5\text{H}_8 \rightarrow \text{C}_5\text{H}_8$	38.4	-13.4	-7.2	-7.6	-5.0	-4.6	0.4	2.1

Table S7: Deviations of the BACKWARD barrier heights of hydrogen transfer reactions for the HTBH38/04 test set for the exchange-correlation functional shown in each column. All quantities are in kcal/mol.

		Expt.	Deviation = Theory - Experiment						
Molecule			LDA	PBE	CAP	NCAP	SCAN	B3LYP	CAM-B3LYP
1	$\text{H} + \text{HCl} \rightarrow \text{H}_2 + \text{Cl}$	8.7	-19.0	-9.8	-7.1	-5.3	-7.9	-4.1	-3.5
2	$\text{OH} + \text{H}_2 \rightarrow \text{H} + \text{H}_2\text{O}$	21.2	-10.4	-8.0	-6.6	-10.9	-10.5	-8.3	-6.1
3	$\text{CH}_3 + \text{H}_2 \rightarrow \text{H} + \text{CH}_4$	15.3	-10.4	-5.9	-5.2	-8.3	-8.3	-5.7	-4.1
4	$\text{OH} + \text{CH}_4 \rightarrow \text{CH}_3 + \text{H}_2\text{O}$	19.6	-17.8	-11.2	-7.5	-7.5	-8.3	-6.1	-4.7
5	$\text{H} + \text{H}_2 \rightarrow \text{H}_2 + \text{H}$	9.6	-12.4	-5.9	-5.3	-7.0	-7.2	-5.3	-4.7
6	$\text{OH} + \text{NH}_3 \rightarrow \text{H}_2\text{O} + \text{NH}_2$	12.7	-24.2	-14.2	-10.3	-9.7	-10.0	-6.1	-3.9
7	$\text{HCl} + \text{CH}_3 \rightarrow \text{Cl} + \text{CH}_4$	7.9	-18.2	-9.7	-7.4	-5.9	-8.5	-3.1	-1.8
8	$\text{OH} + \text{C}_2\text{H}_6 \rightarrow \text{H}_2\text{O} + \text{C}_2\text{H}_5$	19.9	-15.5	-9.6	-5.7	-5.9	-7.4	-4.7	-3.3
9	$\text{F} + \text{H}_2 \rightarrow \text{HF} + \text{H}$	33.4	-8.5	-9.1	-7.4	-12.7	-11.9	-10.6	-8.0
10	$\text{O} + \text{CH}_4 \rightarrow \text{OH} + \text{CH}_3$	8.1	-17.6	-8.9	-6.0	-5.0	-4.9	-3.9	-2.9
11	$\text{H} + \text{PH}_3 \rightarrow \text{PH}_2 + \text{H}_2$	23.2	-13.5	-4.9	-2.2	0.1	-3.6	-0.1	-0.3
12	$\text{H} + \text{HO} \rightarrow \text{H}_2 + \text{O}$	13.1	-25.4	-14.1	-10.4	-9.2	-10.5	-6.5	-6.2
13	$\text{H} + \text{H}_2\text{S} \rightarrow \text{H}_2 + \text{HS}$	17.3	-17.7	-7.8	-5.3	-2.3	-6.0	-1.4	-1.4

Table S7 – continued

14	$\text{O} + \text{HCl} \rightarrow \text{OH} + \text{Cl}$	10.4	-30.1	-18.0	-15.3	-13.2	-11.6	-6.7	-3.3
15	$\text{NH}_2 + \text{CH}_3 \rightarrow \text{CH}_4 + \text{NH}$	22.4	-19.8	-11.5	-7.8	-7.7	-9.9	-5.0	-3.7
16	$\text{NH}_2 + \text{C}_2\text{H}_5 \rightarrow \text{C}_2\text{H}_6 + \text{NH}$	18.3	-19.5	-10.5	-6.5	-6.3	-8.8	-3.5	-2.1
17	$\text{C}_2\text{H}_6 + \text{NH}_2 \rightarrow \text{NH}_3 + \text{C}_2\text{H}_5$	17.4	-14.7	-7.7	-4.2	-3.8	-5.6	-2.2	-0.8
18	$\text{NH}_2 + \text{CH}_4 \rightarrow \text{CH}_3 + \text{NH}_3$	17.8	-18.0	-10.5	-7.1	-6.6	-7.6	-4.7	-3.2
19	$\text{C}_5\text{H}_8 \rightarrow \text{C}_5\text{H}_8$	38.4	-13.4	-7.2	-7.6	-5.0	-4.6	0.4	2.1

Table S8: Deviations of the FORWARD barrier heights of non-hydrogen transfer reactions for the NHTBH38/04 test set for the exchange-correlation functional shown in each column. All quantities are in kcal/mol.

		Expt.	Deviation = Theory - Experiment						
	Molecule		LDA	PBE	CAP	NCAP	SCAN	B3LYP	CAM-B3LYP
1	$\text{H} + \text{N}_2\text{O} \rightarrow \text{OH} + \text{N}_2$	18.14	-15.03	-7.66	-5.53	-8.35	-8.37	-6.31	-4.92
2	$\text{H} + \text{FH} \rightarrow \text{HF} + \text{H}$	42.18	-22.91	-14.24	-11.65	-13.85	-12.57	-10.37	-8.08
3	$\text{H} + \text{ClH} \rightarrow \text{HCl} + \text{H}$	18.00	-15.84	-8.31	-7.09	-8.67	-8.91	-5.51	-3.56
4	$\text{H} + \text{FCH}_3 \rightarrow \text{HF} + \text{CH}_3$	30.38	-16.36	-11.13	-8.60	-12.42	-9.70	-7.95	-4.36
5	$\text{H} + \text{F}_2 \rightarrow \text{HF} + \text{F}$	2.27	28.92	35.65	38.23	34.68	35.91	41.70	-6.96
6	$\text{CH}_3 + \text{FCl} \rightarrow \text{CH}_3\text{F} + \text{Cl}$	7.43	-17.97	-12.96	-7.97	-9.92	-11.41	-8.16	-4.05
7	$\text{F}^- + \text{CH}_3\text{F} \rightarrow \text{FCH}_3 + \text{F}^-$	-0.34	-17.84	-14.16	-8.45	-10.12	-13.31	-8.97	-7.66
8	$\text{F}^- \cdots \text{CH}_3\text{F} \rightarrow \text{FCH}_3 \cdots \text{F}^-$	13.38	-8.19	-7.75	-7.13	-7.67	-7.11	-4.44	-2.61
9	$\text{Cl}^- + \text{CH}_3\text{Cl} \rightarrow \text{ClCH}_3 + \text{Cl}^-$	3.10	-12.54	-9.68	-4.97	-6.80	-9.59	-6.19	-2.77
10	$\text{Cl}^- \cdots \text{CH}_3\text{Cl} \rightarrow \text{ClCH}_3 \cdots \text{Cl}^-$	13.61	-7.79	-7.43	-6.65	-7.64	-6.73	-5.31	-1.73
11	$\text{F}^- + \text{CH}_3\text{Cl} \rightarrow \text{FCH}_3 + \text{Cl}^-$	-12.54	-17.70	-14.10	-8.94	-10.63	-15.18	-9.97	-7.92
12	$\text{F}^- \cdots \text{CH}_3\text{Cl} \rightarrow \text{FCH}_3 \cdots \text{Cl}^-$	2.89	-5.53	-5.30	-5.03	-5.63	-6.53	-4.18	-2.33
13	$\text{OH}^- + \text{CH}_3\text{F} \rightarrow \text{HOCH}_3 + \text{F}^-$	-2.78	-18.18	-14.35	-8.66	-10.13	-13.26	-8.97	-7.24
14	$\text{OH}^- \cdots \text{CH}_3\text{F} \rightarrow \text{HOCH}_3 \cdots \text{F}^-$	10.96	-10.97	-10.56	-9.89	-10.20	-9.31	-6.24	-3.72
15	$\text{H} + \text{N}_2 \rightarrow \text{HN}_2$	14.69	-16.87	-9.38	-8.35	-10.01	-10.38	-7.06	-5.64
16	$\text{H} + \text{CO} \rightarrow \text{HCO}$	3.17	-10.91	-4.90	-3.89	-5.48	-6.84	-3.77	-3.06
17	$\text{H} + \text{C}_2\text{H}_4 \rightarrow \text{CH}_3\text{CH}_2$	1.72	-7.14	-1.83	-0.70	-2.70	-6.19	-1.87	-1.51
18	$\text{CH}_3 + \text{C}_2\text{H}_4 \rightarrow \text{CH}_3\text{CH}_2\text{CH}_2$	6.85	-12.50	-5.28	-1.55	-1.13	-6.19	-0.79	-0.22
19	$\text{HCN} \rightarrow \text{HNC}$	48.16	-3.24	-2.46	-2.96	-2.46	-1.72	-0.68	-0.98

Table S9: Deviations of the BACKWARD barrier heights of non-hydrogen transfer reactions for the NHTBH38/04 test set for the exchange-correlation functional shown in each column. All quantities are in kcal/mol.

		Expt.	Deviation = Theory - Experiment						
	Molecule		LDA	PBE	CAP	NCAP	SCAN	B3LYP	CAM-B3LYP
1	$\text{H} + \text{N}_2\text{O} \rightarrow \text{OH} + \text{N}_2$	83.22	-51.21	-30.94	-27.84	-22.34	-18.60	-10.46	-6.56
2	$\text{H} + \text{FH} \rightarrow \text{HF} + \text{H}$	42.18	-22.91	-14.24	-11.65	-13.85	-12.57	-10.37	-8.08
3	$\text{H} + \text{ClH} \rightarrow \text{HCl} + \text{H}$	18.00	-15.84	-8.31	-7.09	-8.67	-8.91	-5.51	-3.56
4	$\text{H} + \text{FCH}_3 \rightarrow \text{HF} + \text{CH}_3$	57.02	-24.98	-15.83	-10.65	-10.48	-10.36	-8.14	-5.94

Table S9 – continued

5	$\text{H} + \text{F}_2 \rightarrow \text{HF} + \text{F}$	106.18	7.82	19.56	24.69	24.77	30.76	38.81	-9.14
6	$\text{CH}_3 + \text{FCl} \rightarrow \text{CH}_3\text{F} + \text{Cl}$	60.17	-22.45	-18.67	-14.24	-15.95	-14.65	-9.40	-3.60
7	$\text{F}^- + \text{CH}_3\text{F} \rightarrow \text{FCH}_3 + \text{F}^-$	-0.34	-17.84	-14.16	-8.45	-10.12	-13.31	-8.97	-7.66
8	$\text{F}^- \cdots \text{CH}_3\text{F} \rightarrow \text{FCH}_3 \cdots \text{F}^-$	13.38	-8.19	-7.75	-7.13	-7.67	-7.11	-4.44	-2.61
9	$\text{Cl}^- + \text{CH}_3\text{Cl} \rightarrow \text{ClCH}_3 + \text{Cl}^-$	3.10	-12.54	-9.68	-4.97	-6.80	-9.59	-6.19	-2.77
10	$\text{Cl}^- \cdots \text{CH}_3\text{Cl} \rightarrow \text{ClCH}_3 \cdots \text{Cl}^-$	13.61	-7.79	-7.43	-6.65	-7.64	-6.73	-5.31	-1.73
11	$\text{F}^- + \text{CH}_3\text{Cl} \rightarrow \text{FCH}_3 + \text{Cl}^-$	20.11	-10.55	-8.19	-3.06	-4.59	-5.19	-2.36	0.39
12	$\text{F}^- \cdots \text{CH}_3\text{Cl} \rightarrow \text{FCH}_3 \cdots \text{Cl}^-$	29.62	-6.89	-6.89	-5.80	-6.46	-4.03	-1.94	1.33
13	$\text{OH}^- + \text{CH}_3\text{F} \rightarrow \text{HOCH}_3 + \text{F}^-$	17.33	-17.35	-14.21	-8.49	-10.46	-13.26	-8.33	-6.14
14	$\text{OH}^- \cdots \text{CH}_3\text{F} \rightarrow \text{HOCH}_3 \cdots \text{F}^-$	47.20	1.48	-2.86	-1.77	-4.18	-2.40	-0.63	2.52
15	$\text{H} + \text{N}_2 \rightarrow \text{HN}_2$	10.72	-1.57	-1.93	-1.86	-1.70	-1.20	-0.11	0.88
16	$\text{H} + \text{CO} \rightarrow \text{HCO}$	22.68	3.38	1.73	1.75	1.74	1.31	1.72	1.82
17	$\text{H} + \text{C}_2\text{H}_4 \rightarrow \text{CH}_3\text{CH}_2$	41.75	-2.35	-1.41	-0.61	-0.63	1.41	0.12	1.83
18	$\text{CH}_3 + \text{C}_2\text{H}_4 \rightarrow \text{CH}_3\text{CH}_2\text{CH}_2$	32.97	0.24	-3.05	-2.40	-5.14	-2.02	-3.36	0.35
19	$\text{HCN} \rightarrow \text{HNC}$	33.11	-2.24	-2.38	-2.68	-2.32	-0.76	0.45	0.95

Table S10: Deviations of the bond lengths for the test set T96-R for the exchange-correlation functional shown in each column. All quantities are in Å

		Expt.	Deviation = Theory - Experiment						
			LDA	PBE	CAP	NCAP	SCAN	B3LYP	CAM-B3LYP
1	H ₂	0.741	0.025	0.010	0.012	0.008	0.001	0.002	0.004
2	Li ₂	2.673	0.045	0.065	0.120	0.085	0.082	0.037	0.013
3	LiH	1.595	0.011	0.012	0.024	0.016	0.007	-0.001	-0.008
4	LiF	1.564	-0.010	0.012	0.022	0.026	0.005	0.000	-0.006
5	LiCl	2.021	-0.016	0.004	0.019	0.023	0.006	0.000	-0.009
6	LiO	1.688	-0.011	0.011	0.022	0.026	0.005	-0.003	-0.011
7	Be ₂	2.440	-0.030	0.001	0.045	0.039	0.046	0.070	0.265
8	BeH	1.343	0.024	0.019	0.026	0.020	0.011	0.003	0.001
9	BeF	1.361	0.004	0.019	0.025	0.027	0.009	0.010	0.006
10	BeO	1.331	0.002	0.015	0.017	0.019	0.001	-0.005	-0.014
11	BeS	1.742	0.002	0.015	0.017	0.020	0.001	0.002	-0.011
12	B ₂	1.590	0.016	0.029	0.038	0.037	0.028	0.022	0.017
13	BH	1.232	0.025	0.020	0.029	0.022	0.009	0.000	-0.003
14	BF	1.263	-0.002	0.013	0.018	0.020	0.002	0.002	-0.003
15	BF ₃	1.313	-0.002	0.012	0.014	0.018	-0.001	0.003	-0.002
16	BCl	1.715	-0.005	0.016	0.024	0.027	0.004	0.006	-0.007
17	BCl ₃	1.742	-0.012	0.006	0.008	0.015	-0.003	0.004	-0.004
18	BN	1.281	0.042	0.051	0.053	0.056	0.038	0.037	0.028
19	BO	1.204	0.001	0.010	0.012	0.014	0.000	-0.002	-0.007
20	BS	1.609	0.000	0.012	0.014	0.017	0.001	0.001	-0.009
21	C ₂	1.242	0.151	0.162	0.167	0.167	0.006	0.005	0.000
22	CH	1.120	0.021	0.017	0.022	0.019	0.005	0.003	-0.000
23	CH ₄	1.087	0.010	0.009	0.011	0.011	0.001	0.001	0.000
24	CF	1.272	-0.006	0.015	0.016	0.023	0.003	0.003	-0.004

Table S10 – continued

25	CF ₄	1.323	-0.003	0.015	0.015	0.021	-0.001	0.003	-0.003
26	CCl	1.645	-0.010	0.015	0.017	0.026	0.006	0.011	-0.003
27	CCl ₄	1.767	-0.009	0.015	0.014	0.026	0.003	0.014	-0.000
28	CN	1.172	-0.006	0.002	0.004	0.006	-0.009	-0.010	-0.017
29	CO	1.128	-0.000	0.008	0.010	0.012	-0.002	-0.003	-0.008
30	CO ⁺	1.115	-0.000	0.007	0.008	0.010	-0.005	-0.006	-0.011
31	CO ₂	1.160	-1.160	0.011	0.012	0.015	-0.001	-0.000	-0.005
32	CP	1.562	-0.007	0.005	0.006	0.009	-0.010	-0.009	-0.021
33	CS	1.535	-0.002	0.011	0.013	0.016	-0.001	-0.003	-0.015
34	CS ₂	1.553	-1.553	0.009	0.009	0.014	-0.002	0.000	-0.008
35	N ₂	1.098	-0.003	0.005	0.006	0.007	-0.006	-0.007	-0.012
36	N ₂ ⁺	1.116	-0.010	-0.002	-0.001	0.001	-0.011	-0.012	-0.016
37	NH	1.036	0.019	0.015	0.017	0.016	0.004	0.005	0.002
38	NH ⁺	1.070	0.030	0.021	0.023	0.022	0.007	0.008	0.007
39	NF	1.317	-0.013	0.010	0.009	0.019	-0.001	0.001	-0.011
40	NCI	1.611	-0.019	0.007	0.008	0.018	0.004	0.009	-0.005
41	NO	1.151	-0.004	0.007	0.007	0.011	-0.004	-0.006	-0.012
42	NO ⁺	1.063	-0.001	0.007	0.007	0.009	-0.005	-0.007	-0.011
43	NS	1.494	-0.002	0.012	0.012	0.017	-0.002	-0.003	-0.015
44	O ₂	1.208	-0.004	0.011	0.009	0.016	-0.002	-0.004	-0.013
45	O ₂ ⁺	1.116	-0.005	0.006	0.005	0.010	-0.007	-0.010	-0.017
46	OH	0.970	0.016	0.013	0.014	0.015	0.002	0.004	0.003
47	OH ⁺	1.029	0.027	0.019	0.019	0.019	0.005	0.009	0.008
48	OF	1.358	-0.026	0.001	-0.003	0.010	-0.007	-0.009	-0.023
49	F ₂	1.412	-0.027	0.002	-0.004	0.010	-0.012	-0.015	-0.031
50	F ₂ ⁺	1.322	-0.030	-0.006	-0.011	0.001	-0.024	-0.029	-0.044
51	HF	0.917	0.014	0.013	0.013	0.014	0.003	0.005	0.004
52	HF ⁺	1.001	0.028	0.022	0.019	0.021	0.008	0.013	0.013
53	Na ₂	3.079	-0.070	0.000	0.109	0.054	0.043	-0.009	-0.068
54	NaH	1.887	-0.015	0.006	0.030	0.021	0.006	-0.007	-0.020
55	NaF	1.926	-0.022	0.016	0.028	0.031	-0.002	0.002	-0.011
56	NaCl	2.361	-0.031	0.009	0.028	0.032	0.000	0.005	-0.011
57	NaO	2.052	-0.021	0.020	0.033	0.036	0.000	0.000	-0.016
58	MgH	1.730	0.023	0.027	0.030	0.030	0.013	0.012	0.001
59	MgF	1.750	0.006	0.032	0.035	0.041	0.012	0.019	0.009
60	MgCl	2.196	0.002	0.029	0.033	0.042	0.012	0.025	0.010
61	MgO	1.748	-0.022	0.002	0.004	0.010	-0.015	-0.009	-0.024
62	Al ₂	2.466	-0.005	0.023	0.027	0.039	0.009	0.036	0.019
63	AlH	1.648	0.031	0.032	0.037	0.034	0.013	0.013	0.005
64	AlF	1.654	0.005	0.028	0.030	0.036	0.007	0.015	0.007
65	AlCl	2.130	0.006	0.032	0.033	0.044	0.012	0.029	0.013
66	AlO	1.618	-0.005	0.014	0.013	0.020	-0.001	0.007	-0.003
67	AlS	2.029	0.000	0.020	0.017	0.028	-0.000	0.015	-0.002
68	Si ₂	2.246	-0.096	0.040	0.041	0.048	-0.096	-0.087	-0.111
69	SiH	1.520	0.025	0.025	0.029	0.027	0.009	0.009	0.003
70	SiH ₄	1.480	0.013	0.013	0.017	0.014	0.001	-0.000	-0.003

Table S10 – continued

71	SiF	1.601	0.010	0.032	0.032	0.038	0.011	0.018	0.009
72	SiF ₄	1.553	0.008	0.028	0.028	0.033	0.009	0.015	0.008
73	SiCl	2.058	0.002	0.027	0.025	0.037	0.011	0.026	0.011
74	SiCl	2.019	-0.003	0.021	0.021	0.031	0.004	0.017	0.004
75	SiN	1.572	-0.008	0.007	0.008	0.012	-0.005	-0.005	-0.015
76	SiO	1.510	0.005	0.019	0.019	0.023	0.003	0.002	-0.007
77	SiS	1.929	0.006	0.022	0.021	0.028	0.004	0.009	-0.009
78	P ₂	1.893	-0.001	0.013	0.012	0.017	-0.005	-0.004	-0.024
79	P ₄	2.210	-2.210	-0.001	-0.004	0.008	-0.014	-0.006	-0.029
80	PH	1.421	0.021	0.020	0.022	0.021	0.005	0.007	0.001
81	PF	1.589	0.007	0.029	0.028	0.036	0.009	0.016	0.006
82	PCl	2.015	-0.008	0.017	0.014	0.027	0.004	0.019	0.004
83	PN	1.491	-0.004	0.008	0.009	0.012	-0.006	-0.009	-0.021
84	PO	1.476	0.007	0.021	0.020	0.025	0.003	0.004	-0.007
85	S ₂	1.889	0.007	0.022	0.020	0.030	0.006	0.014	-0.005
86	SH	1.341	0.018	0.016	0.017	0.018	0.004	0.006	0.001
87	SF	1.601	-0.003	0.022	0.018	0.030	0.002	0.009	-0.004
88	SF ₆	1.561	-1.561	0.036	0.033	0.044	0.013	0.018	0.006
89	SO	1.481	0.009	0.024	0.023	0.030	0.005	0.009	-0.004
90	SO ₃	1.420	0.009	0.024	0.023	0.029	0.004	0.006	-0.004
91	Cl ₂	1.988	-0.007	0.017	0.012	0.031	0.009	0.023	0.004
92	Cl ₂ ⁺	1.891	0.003	0.023	0.018	0.032	0.008	0.018	-0.003
93	HCl	1.275	0.016	0.014	0.014	0.015	0.004	0.006	0.003
94	HCl ⁺	1.315	0.025	0.018	0.018	0.019	0.006	0.009	0.006
95	ClF	1.628	-0.004	0.023	0.018	0.033	0.005	0.012	-0.004
96	ClO	1.570	-0.015	0.013	0.009	0.023	0.007	0.009	-0.006

Table S11: Deviations of the harmonic vibrational frequencies for the test set T82-F for the exchange-correlation functional shown in each column. All quantities are in cm^{-1}

		Expt.	Deviation = Theory - Experiment						
Molecule			LDA	PBE	CAP	NCAP	SCAN	B3LYP	CAM-B3LYP
1	H ₂	4401.2	-218.6	-85.8	-102.4	-75.5	22.1	17.2	7.6
2	Li ₂	351.4	-17.8	-21.3	-33.5	-27.9	-19.2	-11.2	5.3
3	LiH	1405.7	-29.9	-28.5	-56.2	-39.8	-3.5	5.5	32.2
4	LiF	910.6	13.8	-16.4	-39.1	-40.9	-5.1	7.0	16.9
5	LiCl	643.0	10.6	-3.6	-19.0	-22.3	-7.0	2.5	14.9
6	LiO	814.6	3.7	-18.5	-35.0	-37.5	-8.0	8.7	30.3
7	LiNa	256.8	-4.4	-11.1	-21.5	-18.5	-10.2	-4.5	10.6
8	Be ₂	267.9	99.9	78.7	62.5	52.8	60.6	9.8	-104.5
9	BeH	2060.8	-103.7	-86.3	-99.8	-92.6	-31.7	-23.4	-3.0
10	BeH ⁺	2221.7	-137.9	-112.5	-103.1	-93.0	-25.5	-41.2	-16.0
11	BeF	1247.4	-5.6	-41.2	-56.8	-62.3	-10.6	-11.5	6.2
12	BeCl	846.7	-16.4	-32.7	-41.1	-48.7	-24.7	-29.6	-11.4
13	BeO	1487.3	7.6	-33.2	-36.0	-45.6	29.0	40.1	85.2
14	BeS	997.9	-0.6	-20.4	-23.1	-31.2	21.0	2.8	42.9
15	B ₂	1051.3	-15.1	-39.1	-53.9	-60.4	-46.6	-44.7	-36.9
16	BH	2366.9	-138.0	-124.4	-158.4	-136.5	-47.6	-15.6	21.5
17	BF	1402.1	4.7	-51.0	-66.6	-75.4	-2.3	-1.4	24.5
18	BCl	840.3	-2.7	-31.0	-38.6	-49.5	-3.7	-16.2	14.4
19	BN	1514.6	30.4	1.4	-4.3	-21.5	61.2	54.6	121.6
20	BO	1885.7	2.9	-38.5	-42.2	-57.3	16.6	30.5	69.3
21	BS	1180.2	2.9	-18.5	-19.5	-32.7	28.4	5.9	44.7
22	C ₂	1854.7	45.2	2.2	-5.9	-22.1	44.6	23.0	49.9
23	CH	2858.5	-117.8	-127.1	-148.1	-146.9	-40.0	-35.8	14.4
24	CF	1308.1	24.4	-54.2	-54.8	-80.6	-3.8	-4.3	40.3
25	CN	2068.6	73.0	25.3	20.0	2.4	86.1	86.9	141.1
26	CO	2169.8	11.7	-40.2	-45.5	-60.8	41.6	44.4	88.3
27	CO ⁺	2214.2	37.7	-10.6	-10.1	-33.8	78.6	82.0	133.3
28	CP	1239.7	38.2	9.6	8.6	-5.5	48.2	46.0	89.9
29	CS	1285.2	5.7	-22.9	-24.2	-37.2	23.1	23.6	74.2
30	N ₂	2358.6	43.7	-5.5	-7.7	-24.5	75.9	93.2	145.0
31	N ₂ ⁺	2207.0	114.4	58.8	55.7	34.4	119.1	127.7	167.5
32	NH	3282.3	-133.3	-109.1	-133.7	-130.4	-26.8	-28.3	21.1
33	NF	1141.4	52.9	-9.4	18.9	-35.5	23.4	27.1	71.4
34	NCI	828.0	53.4	8.8	10.1	-11.9	6.2	-2.8	28.7
35	NO	1904.2	56.0	-11.8	0.8	-36.1	56.9	73.1	129.2
36	NO ⁺	2376.4	42.2	-13.7	-12.7	-33.8	87.4	107.0	160.2
37	NS	1218.7	44.1	8.1	11.7	-21.8	43.2	39.0	92.2
38	O ₂	1580.2	42.7	-21.9	-5.7	-48.2	46.4	59.4	125.7
39	O ₂ ⁺	1904.8	98.9	32.3	44.3	4.5	122.7	149.8	217.3
40	OH	3737.8	-143.0	-131.6	-127.9	-154.8	-7.5	-36.5	9.3
41	OH ⁺	3113.4	-211.4	-157.5	-146.9	-158.3	-40.4	-70.0	-49.7

Table S11 – continued

42	F ₂	916.6	144.8	78.2	89.6	60.0	125.6	130.1	179.9
43	F ₂ ⁺	1073.3	142.2	76.5	91.5	56.0	132.0	158.4	222.2
44	HF	4138.3	-148.7	-158.6	-144.1	-177.6	-35.1	-50.9	-19.6
45	HF ⁺	3090.5	-222.4	-178.4	-144.9	-174.9	-61.9	-100.9	-91.5
46	Na2	159.1	3.8	-0.7	-10.5	-8.4	-0.2	-0.8	11.5
47	NaH	1172.2	-3.7	-23.7	-55.9	-42.5	13.8	11.4	39.5
48	NaF	535.7	15.9	-16.5	-31.2	-30.2	7.3	1.5	18.3
49	NaO	492.3	0.8	-24.1	-35.7	-33.2	0.8	-0.6	21.9
50	MgH	1495.2	-92.0	-88.3	-77.1	-88.3	-32.4	-49.1	-3.9
51	MgH ⁺	1699.1	-51.1	-46.4	-39.3	-42.9	20.6	10.8	63.2
52	MgO	784.8	57.4	19.9	17.1	7.1	50.9	34.8	70.2
53	MgS	528.7	15.5	-1.6	-0.8	-10.5	23.0	0.7	24.2
54	Al ₂	350.0	13.0	-8.2	-7.4	-19.1	1.1	-23.7	-12.3
55	AlH	1682.6	-103.1	-100.2	-108.9	-109.9	-41.8	-46.8	-17.2
56	AlF	802.3	-18.8	-50.5	-54.2	-62.0	-10.8	-27.0	-9.8
57	AlCl	481.3	-7.1	-22.5	-22.3	-31.9	-4.2	-21.2	-7.0
58	AlO	979.2	25.6	-19.1	-14.9	-35.1	12.6	-23.0	1.1
59	AlS	617.1	2.5	-15.7	-9.2	-26.9	16.7	-16.9	5.7
60	Si ₂	511.0	39.7	-26.2	-24.0	-33.8	51.9	37.9	68.7
61	SiH	2041.8	-79.5	-92.8	-97.2	-104.6	16.8	-39.4	1.9
62	SiH ⁺	2157.2	-133.8	-114.2	-120.3	-115.3	-50.7	-39.5	-5.4
63	SiF	857.2	-9.1	-45.4	-49.8	-62.9	-11.8	-24.5	-3.2
64	SiCl	535.6	6.5	-13.0	-9.9	-32.7	-11.6	-23.9	-5.2
65	SiN	1151.4	34.3	-1.6	-1.4	-15.2	27.7	29.5	64.1
66	SiO	1241.5	-12.3	-46.9	-45.5	-56.4	11.3	11.5	52.2
67	SiS	749.6	-9.4	-24.2	-21.8	-32.4	7.8	-2.6	33.2
68	P ₂	780.8	15.8	1.4	4.1	-6.4	32.6	29.6	75.2
69	P ₂ ⁺	672.2	12.5	2.4	5.5	-5.5	108.5	99.4	137.2
70	PH	2365.2	-85.2	-78.5	-80.9	-92.5	23.3	-30.1	20.5
71	PF	846.8	0.7	-37.9	-33.4	-49.9	-0.1	-14.1	15.5
72	PCl	551.4	11.4	-19.2	-5.9	-24.4	-4.5	-17.9	5.3
73	PN	1337.2	34.9	2.3	4.2	-9.3	54.7	67.0	123.5
74	PO	1233.3	8.2	-27.3	-22.9	-48.1	22.2	22.8	68.2
75	S ₂	725.6	-5.7	-19.4	-13.9	-33.7	10.6	-6.7	35.4
76	SO	1149.2	-2.2	-40.0	-32.3	-56.5	15.0	6.5	59.1
77	Cl ₂	559.7	8.1	-16.7	-9.5	-31.2	-0.2	-16.2	15.1
78	Cl ₂ ⁺	645.6	3.5	-20.6	-15.2	-33.6	1.2	-8.6	32.6
79	HCl	2990.9	-101.6	-91.1	-87.5	-107.4	-15.0	-42.3	2.7
80	HCl ⁺	2673.7	-139.7	-113.4	-106.4	-108.1	-37.1	-58.6	-19.5
81	ClF	786.1	22.3	-22.7	-13.7	-39.2	4.6	-0.6	38.3
82	ClO	853.8	64.3	9.5	19.1	-11.2	9.5	5.0	41.9

Table S12: Comparison of TDDFT valence and Rydberg excited states of small molecules with experimental values.

Molecule		Exp.	LDA	PBE	CAP	NCAP	B3LYP	CAM-B3LYP
N ₂	V ³ Π _g	8.04	7.57	7.41	7.42	7.54	7.59	7.70
	V ³ Σ _u ⁺	7.75	7.91	7.55	7.51	7.74	7.11	6.98
	V ³ Δ _u	8.88	8.86	8.36	8.41	8.43	8.02	7.94
	V ¹ Π _g	9.31	9.06	9.10	9.13	9.14	9.26	9.38
	V ³ Σ _u ⁻	9.67	9.69	9.69	9.76	9.72	9.35	9.23
	V ¹ Σ _u ⁻	9.92	9.69	9.69	9.76	9.72	9.35	9.23
	V ¹ Δ _u	10.27	10.26	10.11	10.18	10.08	9.75	9.71
	R ³ Σ _g ⁺	12.00	10.40	10.13	10.47	10.72	11.00	11.39
	R ¹ Σ _g ⁺	12.20	10.61	10.41	10.49	10.71	11.30	11.78
	V ³ Π _u	11.19	10.40	10.43	10.51	10.64	10.68	10.81
CO	V ³ Π	6.32	5.96	5.75	5.76	5.98	5.87	5.92
	V ³ Σ ⁺	8.51	8.41	8.11	8.09	8.27	7.94	7.93
	V ¹ Π	8.51	8.17	8.25	8.29	8.32	8.40	8.47
	V ³ Δ	9.36	9.01	8.76	8.82	8.83	8.66	8.68
	R ³ Σ ⁺	10.40	9.19	8.82	9.15	9.97	9.55	9.94
	R ¹ Σ ⁺	10.78	9.20	9.09	9.31	10.19	9.84	10.10
	R ³ Σ ⁺	11.30	9.53	9.36	9.68	10.43	10.16	10.74
	R ¹ Σ ⁺	11.40	9.53	9.43	9.77	10.36	10.05	10.37
	R ³ Π	11.55	9.58	9.44	9.38	10.36	10.27	10.86
	R ¹ Π	11.53	9.60	9.52	9.42	10.50	10.30	10.92
CH ₂ O	V ³ A ₂	3.50	3.06	3.06	3.12	3.18	3.19	3.17
	V ¹ A ₂	3.94	3.67	3.80	3.86	3.87	3.91	3.91
	R ³ B ₂	6.83	5.76	5.56	5.90	6.34	6.28	6.66
	V ³ A ₁	5.53	6.24	5.81	5.81	5.95	5.47	5.38
	R ¹ B ₂	7.09	5.82	5.72	6.06	6.45	6.40	6.81
	R ³ A ₁	7.79	6.45	6.29	6.27	7.02	7.13	7.59
	R ¹ A ₁	7.97	6.46	6.36	6.28	7.02	7.19	7.67
	R ³ B ₂	7.96	6.55	6.39	6.56	7.27	7.08	7.42
	R ¹ B ₂	8.12	6.57	6.46	6.64	7.31	7.15	7.56
	R ¹ A ₂	8.38	6.73	6.63	6.94	7.94	7.43	7.88
C ₂ H ₄	V ³ B _{1u}	4.36	4.63	4.22	4.19	4.36	4.02	3.86
	R ³ B _{3u}	6.98	6.50	6.25	6.65	7.07	6.47	6.77
	R ¹ B _{3u}	7.15	6.55	6.35	6.74	7.13	6.55	6.87
	R ³ B _{2g}	7.79	6.97	6.73	7.02	7.74	7.02	7.46
	R ¹ B _{2g}	8.00	6.99	6.78	7.04	7.80	7.07	7.53
	R ³ B _{1g}	7.79	6.95	6.76	7.08	7.20	7.03	7.39
	R ¹ B _{1g}	7.83	7.00	6.80	7.11	7.70	7.06	7.46
	R ³ A _g	8.15	7.30	7.00	7.19	7.76	7.33	7.73
	R ¹ A _g	8.29	7.35	7.14	7.28	7.82	7.41	7.86
	V ¹ B _{1u}	7.66	7.35	7.24	7.35	7.48	7.31	7.41
MAD			0.87	1.00	0.86	0.48	0.68	0.44

Table S13: Integrated errors of the density, IRD.

System	LDA	PBE	CAP	NCAP	SCAN	B3LYP	CAM-B3LYP
Be ⁰	0.08200	0.03820	0.05286	0.04020	0.07395	0.04905	0.05518
B ³⁺	0.02959	0.01535	0.01145	0.00991	0.00690	0.01206	0.01234
B ⁺	0.05972	0.03291	0.04483	0.03762	0.05296	0.03597	0.04271
C ⁴⁺	0.02483	0.01278	0.00960	0.00830	0.00569	0.00991	0.00989
C ²⁺	0.05055	0.03429	0.04253	0.03847	0.04640	0.03492	0.04008
N ⁵⁺	0.02141	0.01097	0.00827	0.00718	0.00482	0.00841	0.00827
N ³⁺	0.04667	0.03555	0.04177	0.03951	0.04972	0.03519	0.03829
O ⁶⁺	0.01881	0.00960	0.00726	0.00635	0.00420	0.00729	0.00710
O ⁴⁺	0.04575	0.03672	0.04154	0.04011	0.04957	0.03629	0.03797
F ⁷⁺	0.01678	0.00853	0.00647	0.00571	0.00372	0.00643	0.00621
F ⁵⁺	0.04524	0.03778	0.04170	0.04062	0.05074	0.03744	0.03838
Ne ⁸⁺	0.01510	0.00766	0.00583	0.00523	0.00334	0.00577	0.00553
Ne ⁶⁺	0.04492	0.03865	0.04193	0.04109	0.04678	0.03849	0.03904
Ne ⁰	0.13244	0.09647	0.06856	0.08112	0.03530	0.07810	0.08692
AVE	0.04527	0.02967	0.03033	0.02867	0.03101	0.02824	0.03057

$$IRD = \int \left| \rho^{CCSD}(\mathbf{r}) - \rho(\mathbf{r}) \right| d\mathbf{r}$$

Table S14: Integrated errors of the gradient norm of the density, IRG.

System	LDA	PBE	CAP	NCAP	SCAN	B3LYP	CAM-B3LYP
Be ⁰	0.32148	0.15586	0.16329	0.14952	0.15283	0.15260	0.17115
B ³⁺	0.27995	0.13499	0.10124	0.11185	0.07099	0.10827	0.11302
B ⁺	0.32027	0.15866	0.17119	0.16861	0.16502	0.14580	0.16478
C ⁴⁺	0.28719	0.13766	0.10372	0.11480	0.07130	0.10837	0.11207
C ²⁺	0.31616	0.17651	0.19061	0.20711	0.19854	0.16394	0.18120
N ⁵⁺	0.29200	0.13930	0.10585	0.11716	0.07111	0.10836	0.11094
N ³⁺	0.31129	0.20651	0.21966	0.24944	0.24461	0.19244	0.20932
O ⁶⁺	0.29556	0.14108	0.10752	0.11982	0.07172	0.10860	0.11098
O ⁴⁺	0.31063	0.24443	0.25376	0.29336	0.28723	0.22375	0.23915
F ⁷⁺	0.29870	0.14214	0.10866	0.12172	0.07179	0.10852	0.11063
F ⁵⁺	0.31849	0.28438	0.29100	0.33848	0.33656	0.26403	0.27666
Ne ⁸⁺	0.30194	0.14325	0.10966	0.12369	0.07183	0.10850	0.11015
Ne ⁶⁺	0.33743	0.32664	0.33233	0.38598	0.38924	0.30920	0.32142
Ne ⁰	0.79482	0.39219	0.35063	0.35448	0.18928	0.36127	0.38771
AVE	0.34185	0.19883	0.18637	0.20400	0.17086	0.17598	0.18708

$$IRG = \int \left| \left| \nabla \rho^{CCSD}(\mathbf{r}) \right| - \left| \nabla \rho(\mathbf{r}) \right| \right| d\mathbf{r}$$

Table S15: Integrated errors of the laplacian of the density, IRL.

System	LDA	PBE	CAP	NCAP	SCAN	B3LYP	CAM-B3LYP
Be ⁰	1.44692	1.04009	0.85885	1.03432	0.73614	0.92486	0.98664
B ³⁺	1.85724	1.22618	0.94155	1.22268	0.75223	1.02842	1.09172
B ⁺	1.86723	1.40021	1.13998	1.43428	0.98158	1.16239	1.27241
C ⁴⁺	2.33148	1.52719	1.18051	1.52533	0.92163	1.25408	1.33137
C ²⁺	2.25021	1.80818	1.43609	1.87226	1.26014	1.43768	1.54428
N ⁵⁺	2.81362	1.85185	1.43880	1.85907	1.11607	1.50330	1.59419
N ³⁺	2.56208	2.28164	1.79885	2.36620	1.71454	1.78104	1.91733
O ⁶⁺	3.27420	2.12655	1.67398	2.13481	1.24281	1.70010	1.80530
O ⁴⁺	2.78548	2.71851	2.13803	2.89124	2.29757	2.12415	2.29946
F ⁷⁺	3.74831	2.42333	1.90895	2.44143	1.39873	1.91616	2.03899
F ⁵⁺	2.98291	3.25377	2.62453	3.56943	2.90243	2.56502	2.77868
Ne ⁸⁺	4.22930	2.72796	2.15488	2.76740	1.55506	2.14954	2.27676
Ne ⁶⁺	3.11869	3.89047	3.26628	4.36469	3.87346	3.16141	3.39101
Ne ⁰	7.21683	3.91080	3.60618	3.90698	2.42234	3.56509	3.78578
AVE	3.03461	2.29905	1.86910	2.38501	1.65534	1.87666	2.00814

$$IRL = \int \left| \nabla^2 \rho^{CCSD}(\mathbf{r}) - \nabla^2 \rho(\mathbf{r}) \right| d\mathbf{r}$$

Table S16: Dipole moment in Debye

System	CCSD(T)	LDA	PBE	CAP	NCAP	SCAN	B3LYP	CAM-B3LYP
AlF	1.4729	1.4606	1.3739	1.2423	1.3061	1.2985	1.4939	1.4880
BF	0.8194	1.0443	1.0485	1.1074	1.0894	1.0579	0.9503	0.9444
BH ₂ Cl	0.6838	0.4274	0.4379	0.4408	0.4470	0.5430	0.5773	0.6465
BH ₂ F	0.8269	0.6405	0.6182	0.5824	0.5902	0.6813	0.7520	0.7980
BHCl ₂	0.6684	0.4754	0.4815	0.4781	0.4867	0.5578	0.5893	0.6456
BHF ₂	0.9578	0.8070	0.7749	0.7412	0.7487	0.8275	0.8939	0.9347
CH ₂ BH	0.6238	0.4875	0.5090	0.5055	0.5181	0.5647	0.6214	0.6834
CH ₂ BOH	2.2558	2.2752	2.2669	2.2758	2.2739	2.3136	2.2876	2.3217
CH ₃ BH ₂	0.5751	0.7750	0.7259	0.7398	0.7151	0.6942	0.6406	0.6247
CH ₃ BO	3.6779	3.7078	3.6347	3.6307	3.6213	3.7727	3.8022	3.8670
CH ₃ Cl	1.8981	1.8570	1.8196	1.8245	1.8156	1.9208	1.8683	1.9075
CH ₃ F	1.8083	1.6871	1.6370	1.6116	1.6177	1.7025	1.7554	1.8086
CH ₃ Li	5.8304	5.5105	5.4869	5.6440	5.6419	5.7662	5.6434	5.7096
CH ₃ NH ₂	1.3876	1.3625	1.3181	1.3152	1.3126	1.3502	1.3626	1.4080
CH ₃ OH	1.7091	1.6520	1.5951	1.5809	1.5813	1.6496	1.6746	1.7274
CH ₃ SH	1.5906	1.6018	1.5730	1.5915	1.5729	1.6312	1.5718	1.5986
ClCN	2.8496	3.0215	2.9533	2.9392	2.9456	3.0000	3.0059	3.0205
ClF	0.8802	0.7674	0.7192	0.6881	0.6993	0.7978	0.8559	0.9169
CO	0.1172	0.2284	0.2239	0.2431	0.2280	0.1273	0.0871	0.0584
CS	1.9692	2.0942	2.0088	1.9871	1.9889	1.9506	1.9679	1.9747
CSO	0.7327	0.8549	0.7628	0.7253	0.7310	0.8002	0.8502	0.8357
FCN	2.1756	2.3299	2.3228	2.3403	2.3068	2.3381	2.2894	2.2983
FNO	1.6971	1.4491	1.4644	1.4407	1.4568	1.5349	1.5885	1.6377
H ₂ O	1.8601	1.8555	1.7954	1.7958	1.7831	1.8400	1.8548	1.8948
H ₂ O-H ₂ O	2.7303	2.8164	2.7267	2.7288	2.7149	2.7546	2.7661	2.8002
H ₂ O-NH ₃	3.5004	3.6276	3.5086	3.5073	3.4837	3.5311	3.5479	3.5998
H ₂ S-H ₂ S	0.9181	1.0981	1.0315	1.0359	1.0121	1.0176	0.9692	0.9571
H ₂ S-HCl	2.1328	2.3792	2.2779	2.2905	2.2494	2.3041	2.2102	2.2045
HBH ₂ BH	0.8429	0.9079	0.8614	0.8827	0.8479	0.8446	0.8145	0.8535
HBO	2.7322	2.6243	2.5855	2.5690	2.5784	2.7311	2.7863	2.8692
HBS	1.3753	1.2006	1.2268	1.2530	1.2509	1.4045	1.3928	1.5017
HCCCl	0.5009	0.2647	0.2646	0.2744	0.2663	0.3306	0.3503	0.4194
HCCF	0.7452	0.5155	0.4632	0.4412	0.4411	0.5506	0.6276	0.6942
HCHO	2.3927	2.2842	2.2376	2.2055	2.2110	2.3641	2.4017	2.4922
HCl	1.1055	1.1068	1.0681	1.0777	1.0591	1.1249	1.0850	1.1187
HCl-HCl	1.7766	1.8947	1.8196	1.8307	1.8050	1.8691	1.8022	1.8207
HCN	3.0065	3.0034	2.9427	2.9377	2.9371	3.0341	3.0362	3.0937
HCNO	2.956	2.4845	2.4233	2.4076	2.4103	2.5996	2.7592	2.9519
HCOF	2.1169	2.0312	1.9867	1.9756	1.9809	2.0948	2.1236	2.1863
HCONH ₂	3.9152	3.9059	3.8264	3.8457	3.8348	3.9415	3.9587	4.0305
HCOOH	1.3835	1.4175	1.4171	1.4375	1.4374	1.4812	1.4617	1.4772
HF	1.8059	1.7949	1.7455	1.7412	1.7328	1.7851	1.7998	1.8248
HF-HF	3.3991	3.4460	3.3552	3.3508	3.3390	3.4064	3.4215	3.4552

Table S16 – continued

HN3	1.6603	1.8209	1.7542	1.7606	1.7447	1.7479	1.7009	1.6801
HNC	3.0818	3.1358	3.0654	3.0803	3.0617	3.0530	3.0047	3.0146
HNCO	2.0639	2.0324	1.9660	1.9857	1.9520	2.0396	2.0453	2.0843
HOCl	1.5216	1.5306	1.4974	1.5031	1.4915	1.5321	1.5235	1.5409
HOCN	3.7998	3.9575	3.8703	3.9082	3.8971	3.9549	3.9149	3.9402
HOOH	1.5732	1.5681	1.5239	1.5190	1.5109	1.5533	1.5719	1.6003
LiBH4	6.1281	5.9096	5.9476	6.0182	6.0280	6.0738	6.0251	6.0483
LiCl	7.096	6.8277	6.8442	6.9350	6.9284	7.0322	6.9457	7.0052
LiCN	6.9851	6.8047	6.8165	6.9036	6.9086	6.9579	6.8966	6.9244
LiF	6.2879	6.0867	6.0935	6.1477	6.1478	6.2168	6.1915	6.2172
LiH	5.8286	5.6099	5.6155	5.7501	5.7669	5.8493	5.7254	5.7729
LiOH	4.5664	4.3194	4.3768	4.4652	4.4643	4.5098	4.4456	4.4543
N2H4	2.7179	2.7282	2.6368	2.6388	2.6237	2.6693	2.7014	2.7745
NaCl	9.0066	8.4917	8.4901	8.7538	8.7413	8.8427	8.6792	8.8073
NaCN	8.8903	8.5613	8.5643	8.7581	8.7559	8.8039	8.7082	8.7756
NaF	8.1339	7.7622	7.7239	7.8951	7.9036	7.9817	7.9369	8.0066
NaH	6.3966	5.6711	5.7562	6.1936	6.0641	6.3337	6.0291	6.2841
NaOH	6.769	6.4907	6.5523	6.6709	6.6791	6.6753	6.6325	6.6354
NH2Cl	1.9468	1.9478	1.9180	1.9293	1.9171	2.0039	1.9494	1.9706
NH2F	2.2688	2.2072	2.1472	2.1361	2.1337	2.2572	2.2575	2.3153
NH2OH	0.7044	0.6543	0.6306	0.6205	0.6247	0.7007	0.6913	0.7242
NH3	1.5289	1.5265	1.4748	1.4826	1.4683	1.5090	1.5203	1.5683
NH3-BH3	5.281	5.2789	5.2510	5.2855	5.2698	5.3152	5.2714	5.3069
NH3-NH3	2.1345	2.2229	2.1436	2.1474	2.1323	2.1623	2.1654	2.2036
NH3O	5.3942	5.1549	5.0477	5.0407	5.0382	5.1806	5.2447	5.4048
OC12	0.5625	0.5154	0.4656	0.4546	0.4549	0.4942	0.5545	0.6083
P2H4	0.9979	1.0190	0.9672	1.0086	0.9549	1.0243	0.9347	1.0041
PH2OH	0.6836	0.6516	0.6610	0.6424	0.6675	0.6432	0.7182	0.7043
PH3	0.6069	0.6504	0.6025	0.6438	0.5917	0.6429	0.5568	0.6061
PH3O	3.7704	3.5852	3.4760	3.4500	3.4542	3.6008	3.7172	3.8596
S2H2	1.1425	1.1393	1.0913	1.1106	1.0811	1.1485	1.0971	1.1493
SCl2	0.3891	0.2953	0.2995	0.2782	0.2978	0.3439	0.3808	0.4049
SF2	1.0555	0.8444	0.7973	0.7481	0.7716	0.8564	1.0029	1.0681
SH2	0.9939	1.0114	0.9656	0.9884	0.9557	1.0126	0.9618	1.0075
SiH3Cl	1.3645	1.2625	1.2104	1.1960	1.1958	1.2488	1.2892	1.3484
SiH3F	1.3123	1.2394	1.1743	1.1354	1.1359	1.2030	1.2686	1.3123
SiO	3.1123	2.9840	2.9017	2.8195	2.8737	3.0029	3.2087	3.3328
SO2	1.6286	1.5218	1.4850	1.4437	1.4713	1.5389	1.6655	1.7371
AlH2	0.4011	0.3405	0.3481	0.3552	0.3795	0.3992	0.4482	0.4378
BeH	0.2319	0.1988	0.2434	0.2709	0.2766	0.2866	0.3050	0.2799
BH2	0.5004	0.5376	0.5102	0.5034	0.5050	0.4699	0.4921	0.5110
BN	2.0366	1.8504	1.8899	1.9384	1.8910	2.1672	2.1340	2.2778
BO	2.3171	2.2075	2.1837	2.1937	2.1836	2.3566	2.4217	2.5003
BS	0.7834	0.6130	0.6599	0.7174	0.6829	0.8825	0.8422	0.9445
C2H	0.7601	0.7798	0.7625	0.7466	0.7699	0.7514	0.7610	0.7629
C2H3	0.6867	0.7796	0.7214	0.7160	0.7178	0.6786	0.6984	0.7069

Table S16 – continued

C2H5	0.314	0.4465	0.3808	0.3722	0.3683	0.3319	0.3413	0.3368
CF	0.6793	0.9598	0.9422	0.9671	0.9549	0.8503	0.7727	0.7433
CF2	0.5402	0.7846	0.7623	0.8054	0.7846	0.7208	0.6212	0.6002
CH2F	1.3796	1.1652	1.1533	1.1391	1.1405	1.2648	1.3009	1.3583
CH2PH	0.8748	0.8986	0.8990	0.9460	0.9102	0.9951	0.8574	0.8587
CH2-t	0.5862	0.6244	0.5896	0.5815	0.5848	0.5636	0.5941	0.6149
CH3O	2.0368	2.3031	2.1216	2.0939	2.0870	2.0598	2.0916	2.1171
ClO2	1.8627	1.7008	1.6696	1.6400	1.6607	1.7237	1.8304	1.9069
CN	1.4318	1.1365	1.1546	1.1712	1.1283	1.4595	1.3667	1.5438
FCO	0.7678	0.7467	0.7572	0.7708	0.7630	0.8635	0.8306	0.8674
FH-BH2	2.973	3.1439	3.0208	2.9812	2.9699	2.9897	3.0340	3.0654
FH-NH2	4.6265	4.6736	4.5641	4.5629	4.5349	4.6489	4.6533	4.7182
FH-OH	3.3808	3.2260	3.2676	3.2834	3.2643	3.3917	3.4039	3.4433
H2CN	2.4939	2.5728	2.4666	2.4563	2.4523	2.5084	2.5015	2.5468
H2O-Al	4.3573	4.1925	4.2175	4.4188	4.3426	4.4480	4.2751	4.3717
H2O-Cl	2.2383	3.2621	3.1191	3.1602	3.1260	2.9277	2.7610	2.5301
H2O-F	2.1875	3.3489	3.1722	3.1600	3.1465	2.8458	2.8303	2.6667
H2O-Li	3.6184	1.7386	2.3975	3.1190	2.5400	2.7992	2.4949	3.1559
HCHS	1.7588	1.6660	1.6712	1.6957	1.6878	1.8378	1.7376	1.7818
HCO	1.6912	1.6015	1.5537	1.5429	1.5421	1.6793	1.7091	1.7877
HCP	0.3542	0.3455	0.3710	0.4229	0.3911	0.4530	0.3109	0.2825
HNO	1.6536	1.5716	1.4845	1.4728	1.4615	1.5600	1.6249	1.7210
HNO2	1.9345	1.9462	1.8829	1.8888	1.8757	1.9506	1.9564	1.9910
HNS	1.4062	1.3763	1.3359	1.3360	1.3282	1.3686	1.3802	1.4178
HO2	2.1659	2.3070	2.2112	2.2052	2.1955	2.1340	2.1803	2.1956
HPO	2.6291	2.3223	2.2390	2.1939	2.2155	2.3434	2.4871	2.6156
LiN	7.0558	6.5415	6.5489	6.7133	6.7297	6.8840	6.8172	6.9743
N2H2	2.8771	2.8730	2.7650	2.7625	2.7461	2.8025	2.8452	2.9288
NCI	1.1279	1.3736	1.2727	1.2292	1.2588	1.1267	1.1990	1.1832
NCO	0.7935	0.8677	0.8619	0.8630	0.8640	0.8641	0.7998	0.7793
NF	0.0671	0.3403	0.3136	0.3118	0.3197	0.1586	0.1385	0.0996
NF2	0.1904	0.0079	0.0318	0.0163	0.0268	0.1429	0.1664	0.1924
NH	1.5433	1.5308	1.4815	1.4776	1.4701	1.5281	1.5219	1.5624
NH2	1.7853	1.7833	1.7201	1.7227	1.7107	1.7644	1.7698	1.8209
NO	0.1271	0.2449	0.2292	0.2340	0.2294	0.1199	0.1152	0.0894
NO2	0.335	0.2802	0.2753	0.2619	0.2628	0.3100	0.3499	0.3885
NOC1	2.0773	1.6328	1.7388	1.7735	1.7777	1.8447	1.8005	1.8738
NP	2.8713	2.8142	2.7212	2.6711	2.6999	2.7648	2.9212	3.0457
NS	1.8237	1.8609	1.7674	1.7327	1.7460	1.7200	1.8324	1.8891
OC1	1.279	1.4566	1.3439	1.3130	1.3217	1.2061	1.3235	1.3351
OF	0.0205	0.2491	0.1938	0.1957	0.1721	0.0324	0.0140	0.0240
OF2	0.3252	0.2654	0.2795	0.2696	0.2788	0.3254	0.3315	0.3395
OH	1.655	1.6478	1.5940	1.5905	1.5824	1.6412	1.6452	1.6783
PC1	0.5657	0.2803	0.3086	0.2835	0.2924	0.4024	0.4695	0.5603
PF	0.8104	0.6045	0.5715	0.5171	0.5376	0.6164	0.7547	0.8114
PH	0.4375	0.4472	0.4202	0.4458	0.4138	0.4750	0.4007	0.4366

Table S16 – continued

PH2	0.5472	0.5786	0.5357	0.5713	0.5255	0.5891	0.5008	0.5473
PO	1.9617	1.8240	1.7658	1.7106	1.7407	1.8685	2.0303	2.1496
PO2	1.4426	1.2857	1.2608	1.2305	1.2374	1.3785	1.4312	1.5265
PPO	1.8812	1.7935	1.6797	1.6082	1.6429	1.7665	1.9464	2.0145
PS	0.6825	0.4795	0.4938	0.4737	0.4893	0.6027	0.6423	0.7491
SCI	0.069	0.2249	0.1797	0.1909	0.1853	0.0468	0.0361	0.0544
SF	0.8139	0.5677	0.5423	0.5011	0.5167	0.6300	0.7477	0.8212
SH	0.7727	0.7806	0.7449	0.7617	0.7377	0.7960	0.7462	0.7821
SO-trip	1.5606	1.4036	1.3581	1.3154	1.3329	1.3927	1.5320	1.6299
MAD		0.1589	0.1529	0.1413	0.1430	0.0892	0.0750	0.0670

Table S17: Static and dynamic polarizabilities in a.u.

System	Freq a.u.	Reff	LDA	PBE	CAP	NCAP
MC-SCF						
H ₂ O	0.00	9.210	10.12	10.14	9.46	9.60
	0.05	9.284	10.22	10.25	9.55	9.70
	0.10	9.520	10.58	10.62	9.85	10.00
	0.15	9.960	11.33	11.41	10.45	10.62
	0.20	10.770	13.07	13.36	11.73	11.94
	0.25	12.560	174.40	-8.91	19.38	19.53
NH ₃	0.00	13.880	14.83	14.75	13.80	14.01
	0.05	14.047	15.05	14.97	13.97	14.20
	0.10	14.600	15.80	15.74	14.57	14.82
	0.15	15.784	17.65	17.71	15.95	16.24
	0.20	18.840	29.24	34.42	21.04	21.33
CH ₄	0.00	15.616	17.49	17.22	16.35	16.42
	0.05	15.740	17.66	17.39	16.49	16.56
	0.10	16.129	18.20	17.92	16.95	17.02
	0.15	16.836	19.22	18.93	17.80	17.87
	0.20	17.976	20.96	20.65	19.23	19.30
	0.25	19.798	24.12	23.82	21.71	21.74
HF	0.30	22.933	31.96	31.96	27.14	26.87
	0.00	5.324	5.89	5.94	5.56	5.62
	0.10	5.429	6.05	6.12	5.70	5.76
	0.20	5.795	6.68	6.79	6.23	6.30
	0.30	6.692	9.26	9.98	8.09	8.12
H ₂	0.40	17.012	6.68	7.09	5.50	5.33
	0.00	5.203	5.56	5.34	5.20	5.20
	0.10	5.392	5.78	5.55	5.39	5.39
	0.20	6.061	6.59	6.31	6.08	6.08
	0.30	7.740	8.67	8.24	7.80	7.80
CCSD						
N ₂	0.0000	11.60	11.81	11.76	11.28	11.41
	0.0720	11.75	11.99	11.94	11.44	11.57
	0.0886	11.83	12.08	12.03	11.52	11.66
	0.0934	11.84	12.11	12.06	11.55	11.68
	0.0995	11.89	12.15	12.10	11.59	11.72
CO	0.0000	13.07	13.40	13.36	12.72	12.81
	0.0720	13.32	13.70	13.66	12.98	13.07
	0.0886	13.46	13.86	13.81	13.12	13.22
	0.0934	13.5	13.91	13.87	13.16	13.26
	0.0995	13.57	13.99	13.94	13.23	13.33
CO ₂	0.0000	18.00	17.44	17.51	16.71	16.88
	0.0720	18.27	17.70	17.78	16.95	17.12
	0.0886	18.42	17.85	17.93	17.08	17.25

Table S17 – continued

	0.0934	18.46	17.89	17.98	17.13	17.30
	0.0995	18.53	17.96	18.04	17.18	17.36
Cl ₂	0.0000	30.86	30.37	30.04	28.73	29.24
	0.0720	31.52	31.08	30.75	29.34	29.88
	0.0886	31.89	31.50	31.15	29.69	30.24
	0.0934	32.01	31.64	31.29	29.81	30.37
	0.0995	32.18	31.86	31.50	29.97	30.54
C ₂ H ₂	0.0000	22.25	23.38	23.29	21.94	22.32
	0.0720	22.82	24.07	24.00	22.53	22.93
	0.0886	23.14	24.44	24.38	22.85	23.27
	0.0934	23.24	24.57	24.51	22.96	23.38
	0.0995	23.38	24.74	24.69	23.10	23.53
OCS	0.0000	35.71	34.08	34.01	32.37	32.90
	0.0720	36.80	35.11	35.04	33.27	33.84
	0.0886	37.36	35.67	35.60	33.77	34.36
	0.0934	37.57	35.86	35.79	33.93	34.53
	0.0995	37.88	36.12	36.05	34.16	34.77
CS ₂	0.0000	59.15	54.40	54.25	51.56	52.46
	0.0720	62.04	56.89	56.74	53.79	54.77
	0.0886	63.77	58.31	58.16	55.05	56.08
	0.0934	64.40	58.80	58.65	55.49	56.52
	0.0995	65.20	59.48	59.33	56.09	57.15
MAD			4.44	2.25	1.92	1.74

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